

Method for object motion characteristic estimation based on wavelet Multi-Resolution Analysis: MRA

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Abstract—Method for object motion characteristic estimation based on wavelet Multi-Resolution Analysis: MRA is proposed. With moving pictures, the motion characteristics, direction of translation, roll/pitch/yaw rotations can be estimated by MRA with an appropriate support length of the base function of wavelet. Through simulation study, method for determination of the appropriate support length of Daubechies base function is clarified. Also it is found that the proposed method for object motion characteristics estimation is validated.

Keywords-object motion characteristic; MRA; wavelet.

I. INTRODUCTION

There are some conventional methods for object detections and object motion characteristics estimations. Optical flow, template matching is well known as the method for object motion characteristic estimations. On the other hands, the method for motion characteristic estimation based on wavelet MRA is also widely used [1]-[9]. Wavelet base function is defined with support length. The most appropriate support length depends on the motion characteristic [10],[11]. Therefore, it is necessary to determine an appropriate support length for estimation of motion characteristics. Meanwhile, it is required to estimate motion characteristics such as translation vector, speed and direction, rotation, direction and speed (rotation angle). 3D object motion characteristics is estimated based on wavelet analysis as well [12].

The method proposed here is based on wavelet MRA with an appropriate support length which is determined by the proposed method and allows estimation of motion characteristics with moving picture. Through simulation study, it is confirmed that the method for appropriate support length is valid together with the method for motion characteristic estimations.

The following section describes the proposed method followed by the simulation study.

II. PROPOSED METHOD

A. Process Flow of the Proposed Method

Figure 1 shows Process flow of the proposed motion characteristic estimations based on wavelet MRA with appropriate support length of base function which is determined by the proposed method. Acquired moving picture is essentially represented in three dimensional space. From the

moving picture, the most appropriate support length is determined based on the proposed method which is described in the next sub-section. Then 3D wavelet MRA is applied to the acquired moving picture. As the results from the MRA, motion characteristics are estimated.

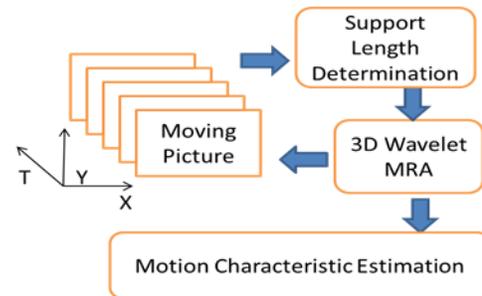


Figure 1 Process flow of the proposed motion characteristic estimations based on wavelet MRA with appropriate support length of base function which is determined by the proposed method

B. Wavelet Multi-Resolution Analysis: MRA

Two dimensional wavelet transformations is defined by equation (1).

$$F = [C_n [C_m f_{xy}]'] \quad (1)$$

where C_m denotes another wavelet transformation matrix while f_{xy} denotes two dimensional data of image. As the result, $F=(LL_1, LH_1, HL_1, HH_1)$ with four frequency components in x and y directions, LL_1, LH_1, HL_1, HH_1 . C_n can be determined with the method which is described in the second paragraph of this sub-section. Therefore, $C_n C_n^t=I$. Then f is converted to $F_1=(L_1, H_1)$, $F_2=C_n L_1=(L_2, H_2)$, $F_3=C_n L_2=(L_3, H_3)$, and $F_m=C_n L_{m-1}=(L_m, H_m)$.

This process is referred to “Decomposition”. Also f is reconstructed as $C_n^{-1} F_m = C_n^{-1} (L_m, H_m) = L_{m-1}, \dots, C_n^{-1} F_2 = L_1, C_n^{-1} F_1 = f$. This process is referred to “Reconstruction”. There are some based functions such as Haar, Daubechies, etc. Through the preliminary simulation study with radar echo data, Daubechies base function is selected. Daubechies base function is defined as $\{\alpha_k\}$ satisfying the following three conditions,

$$\phi(x) = \sum_k \alpha_k \sqrt{2} \phi(2x - k) \quad (2)$$

$$\beta_k = (-1)^k \alpha_{1-k} \quad (3)$$

$$\varphi(x) = \sum_k \beta_k \sqrt{2} \phi(2x-k) \quad (4)$$

where equation (2) is referred to scaling function while equation (4) is referred to wavelet function, respectively. There is two-scale relation between the scaling function and the wavelet function. Also, k denotes support length.

Example of the scaling function and wavelet function with support length of four is as follows,

$$\phi(x) = \frac{1+\sqrt{3}}{4\sqrt{2}}\phi(2x-0) + \frac{3+\sqrt{3}}{4\sqrt{2}}\phi(2x-1) + \frac{3-\sqrt{3}}{4\sqrt{2}}\phi(2x-2) + \frac{1-\sqrt{3}}{4\sqrt{2}}\phi(2x-3)$$

$$\psi(x) = \frac{1-\sqrt{3}}{4\sqrt{2}}\psi(2x-0) - \frac{3-\sqrt{3}}{4\sqrt{2}}\psi(2x-1) + \frac{3+\sqrt{3}}{4\sqrt{2}}\psi(2x-2) - \frac{1+\sqrt{3}}{4\sqrt{2}}\psi(2x-3)$$

Both functions are shown in Figure 2.

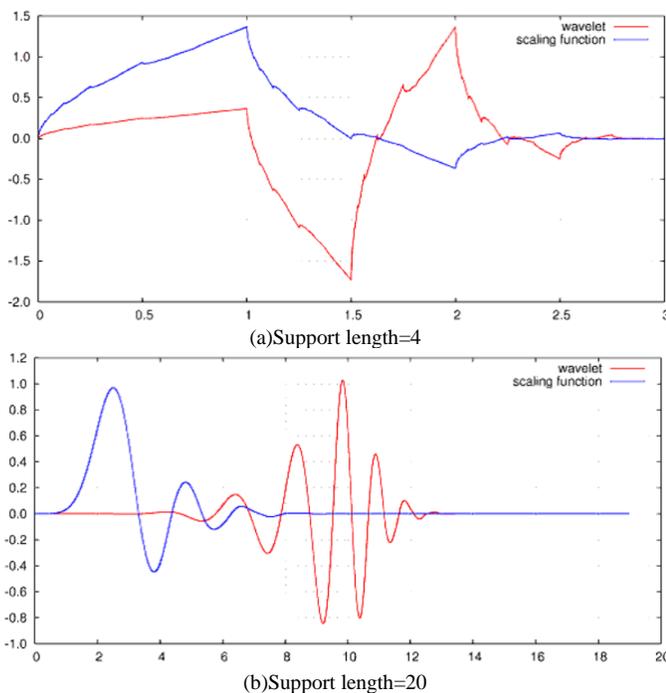


Figure 2 Scaling and wavelet functions with the different support length.

Method for determination of Daubechies wavelet coefficients is as follows,

For instance, the 8th order¹ of Daubechies base function based C_n with the support length of two can be expressed with the equation (5).

$$C_8^{[2]} = \begin{bmatrix} \eta_1 \\ \eta_2 \\ \eta_3 \\ \eta_4 \\ \eta_5 \\ \eta_6 \\ \eta_7 \\ \eta_8 \end{bmatrix} = \begin{bmatrix} p_0 & p_1 & & & & & & \\ q_0 & q_1 & & & & & & \\ & & p_0 & p_1 & & & & \\ & & q_0 & q_1 & & & & \\ & & & & p_0 & p_1 & & \\ & & & & q_0 & q_1 & & \\ & & & & & & p_0 & p_1 \\ & & & & & & q_0 & q_1 \end{bmatrix} \begin{bmatrix} \eta_1 \\ \eta_2 \\ \eta_3 \\ \eta_4 \\ \eta_5 \\ \eta_6 \\ \eta_7 \\ \eta_8 \end{bmatrix}$$

$$= \begin{bmatrix} p_0x_1 + p_1x_2 \\ q_0\eta_1 + q_1\eta_2 \\ p_0\eta_3 + p_1\eta_4 \\ q_0\eta_3 + q_1\eta_4 \\ p_0\eta_5 + p_1\eta_6 \\ q_0\eta_5 + q_1\eta_6 \\ p_0\eta_7 + p_1\eta_8 \\ q_0\eta_7 + q_1\eta_8 \end{bmatrix} \quad (5)$$

where $[n]$ denotes support length. The 8th order of C_n with the support length of four is also expressed with the equation (6).

$$C_8^{[4]} = \begin{bmatrix} \eta_1 \\ \eta_2 \\ \eta_3 \\ \eta_4 \\ \eta_5 \\ \eta_6 \\ \eta_7 \\ \eta_8 \end{bmatrix} = \begin{bmatrix} p_0 & p_1 & p_2 & p_3 & & & & \\ q_0 & q_1 & q_2 & q_3 & & & & \\ & & p_0 & p_1 & p_2 & p_3 & & \\ & & q_0 & q_1 & q_2 & q_3 & & \\ & & & & p_0 & p_1 & p_2 & p_3 \\ & & & & q_0 & q_1 & q_2 & q_3 \\ p_2 & p_3 & & & & & p_0 & p_1 \\ q_2 & q_3 & & & & & q_0 & q_1 \end{bmatrix} \begin{bmatrix} \eta_1 \\ \eta_2 \\ \eta_3 \\ \eta_4 \\ \eta_5 \\ \eta_6 \\ \eta_7 \\ \eta_8 \end{bmatrix}$$

$$= \begin{bmatrix} p_0\eta_1 + p_1\eta_2 + p_2\eta_3 + p_3\eta_4 \\ q_0\eta_1 + q_1\eta_2 + q_2\eta_3 + q_3\eta_4 \\ p_0\eta_5 + p_1\eta_6 + p_2\eta_7 + p_3\eta_8 \\ q_0\eta_5 + q_1\eta_6 + q_2\eta_7 + q_3\eta_8 \\ p_0\eta_5 + p_1\eta_6 + p_2\eta_7 + p_3\eta_8 \\ q_0\eta_5 + q_1\eta_6 + q_2\eta_7 + q_3\eta_8 \\ p_0\eta_7 + p_1\eta_8 + p_2\eta_1 + p_3\eta_2 \\ q_0\eta_7 + q_1\eta_8 + q_2\eta_1 + q_3\eta_2 \end{bmatrix} \quad (6)$$

p_i and q_i in the equations (5) and (6) is also expressed with equation (7) and (8), respectively.

$$(C_n^{[2]})^T C_n^{[2]} = I_n$$

$$p_0 + p_1 = \sqrt{2} \quad (7)$$

$$q_0 = p_1$$

$$q_1 = -p_0$$

$$0^0 q_0 + 1^0 q_1 = 0$$

¹ Scalar data consist of eight numerical data, η_1 to η_8 is assumed.

$$\begin{aligned} (C_n^{[4]})^T C_n^{[4]} &= I_n \\ p_0 + p_1 + p_2 + p_3 &= \sqrt{2} \\ q_0 &= p_3 \\ q_1 &= -p_2 \\ q_2 &= p_1 \\ q_3 &= -p_0 \end{aligned} \quad (8)$$

$$0^0 q_0 + 1^0 q_1 + 2^0 q_2 + 3^0 q_3 = 0$$

$$0^1 q_0 + 1^1 q_1 + 2^1 q_2 + 3^1 q_3 = 0$$

These equations can be expanded to the general support length of C_n as shown in equation (9).

$$\begin{aligned} (C_n^{[sup]})^T C_n^{[sup]} &= I_n \\ \sum_{j=0}^{sup-1} p_j &= \sqrt{2} \\ q_j &= (-1)^j p_{(sup-1)-j} \quad (j=0,1,2,\dots,(sup-1)) \\ \sum_{j=0}^{sup-1} j^r q_j &= 0 \quad \left(r=0,1,2,\dots,\left(\frac{sup}{2}-1\right) \right) \end{aligned} \quad (9)$$

Therefore, the coefficients of the Daubechies base function can be determined from the solution of the equation (9).

C. Method for Most Appropriate Support Length Determinations

Figure 3 shows process flow of the proposed most appropriate support length determination method.

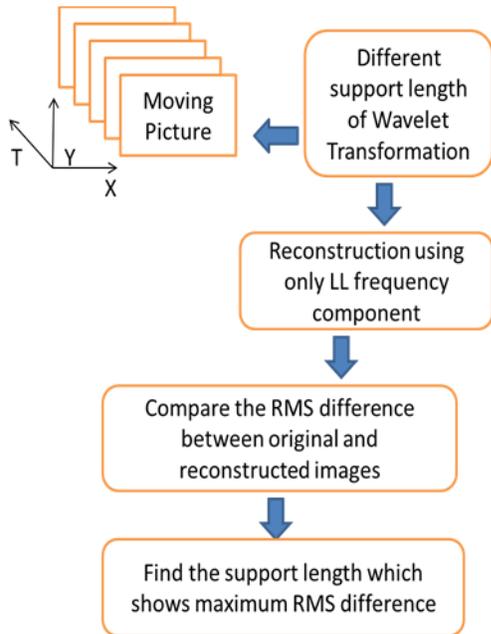


Figure 3 Method for the most appropriate support length determinations

Wavelet transformation with the different support length is applied to the original image. Then reconstruct the image with the decomposed images of LL component only. If the original image does not have any high frequency components, then LL component is totally equal to the original image. It is not always. Usually, most images have some extent of high frequency components results in the reconstructed image with

LL component only is different from the original image obviously.

High frequency components are depends on the spatially and temporally changes in the original image. Therefore, if the Root Mean Square: RMS difference between the reconstructed and the original image is zero, then it may say that there is no high frequency component in the original image. Nevertheless the original image contains relatively large high frequency components, RMS difference is small then it may also say that the spatial and temporal changes cannot be extracted effectively. Consequently, it may say that the support length of which wavelet transformation with the different support length of base function is applied to the original image is the most appropriate if the RMS difference is maximum.

III. SIMULATION STUDY

A. Simulation Data Used

32 frames of time series of shuttlecock like simulation images are crated with PovRay of Computer Graphics software. Translations in vertical, horizontal, and slant directions, and the rotations in pitch, roll, and yaw directions are taken into account as motion characteristics. One of the examples of the moving picture of shuttlecock for the rotation in pitch direction is shown in Figure 4.



Figure 4 Example of the moving picture of shuttlecock for the rotation in pitch direction

B. Simulation Procedure

2D wavelet transformation is applied to the simulation data of moving pictures. Then the reconstructed images are created with HL, LH, and HH components only. Thus the changed pixels or edge pixels are extracted. The changed pixels are counted after the thresholding (binarizing) with an appropriate threshold.

C. Simulation Results

Figure 5 shows the number of changed pixels in the directions of vertical (Red), horizontal (Blue), and slant (Green), respectively when the shuttlecock moves in the directions of vertical, horizontal, and slant (45 degree). The resultant graphs are quite reasonable. In this case, the changed pixels are extracted based on the wavelet transformation with the Daubechies base function of support length of two. Therefore, it is possible to find the moving directions easily. On the other hands, Figure 6 shows the number of changed pixels when the shuttlecock moves in horizontal direction. In this case, the changed pixels are extracted based on the wavelet transformation with the Daubechies base function of the different support length, 2, 4, and 8.

Figure 6 (a), (b), and (c) shows the number of changed pixels extracted from the wavelet transformation with the Daubechies base function of the support length of 2, 4, and 8, respectively.

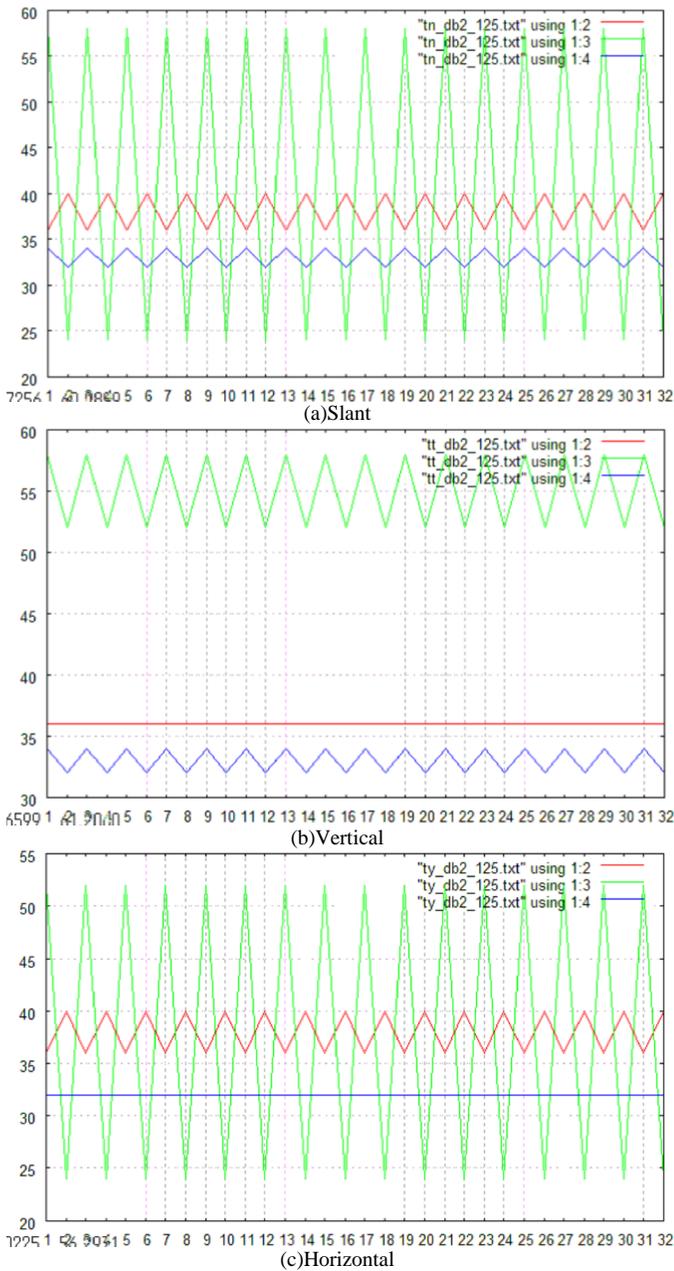


Figure 5 The number of changed pixels in the directions of vertical (Red), horizontal (Blue), and slant (Green), respectively when the shuttlecock moves in the directions of vertical, horizontal, and slant (45 degree). Changed pixels are extracted based on the wavelet transformation with support length of two.

It is quite obvious that the extracted changed pixels depend on the support length as shown in Figure 6. Also, it is found that support length of 4 is the most appropriate.

Figure 7 shows the number of changed pixels in the directions of slant, vertical, and horizontal. In this case, shuttlecock rotates from 0 to 360 degrees in pitch direction.

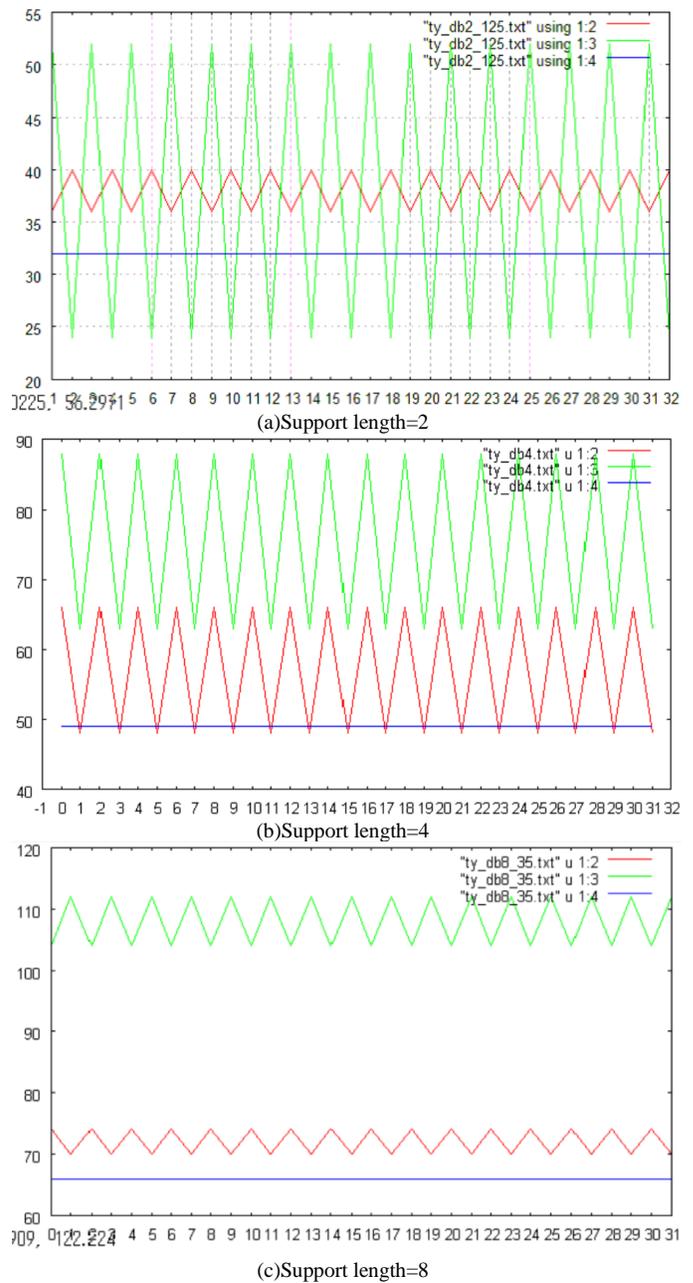
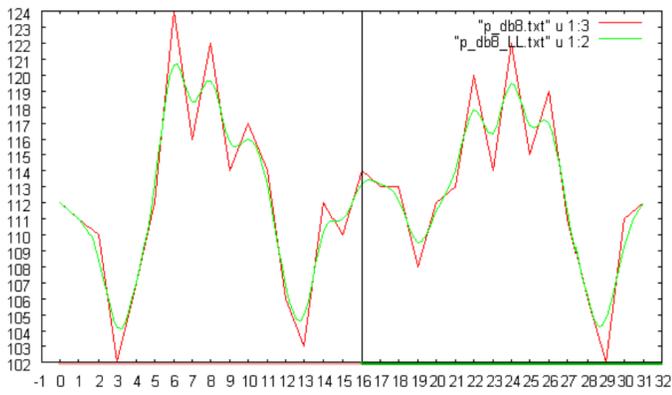
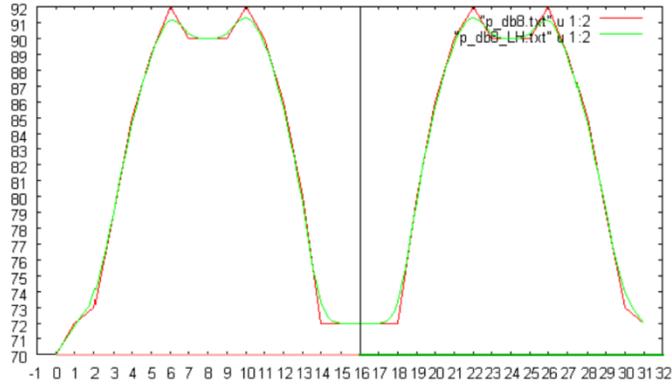


Figure 6 The number of changed pixels when the shuttlecock moves in horizontal direction. In this case, the changed pixels are extracted based on the wavelet transformation with the Daubechies base function of the different support length, 2, 4, and 8.

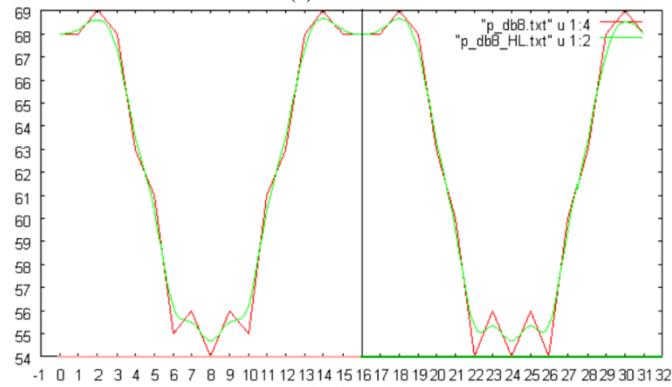
The changed pixels are extracted based on the wavelet transformation with the Daubechies base function of support length of 8. Meanwhile, Figure 8 (a), (b), and (c) shows the number of changed pixels in vertical direction, for the support length of 2, 4, and 8, respectively. Figure 9 (a), (b), and (c) shows the number of changed pixels when the shuttlecock is rotated by 180, 360, and 720 degrees, respectively.



(a)Slant

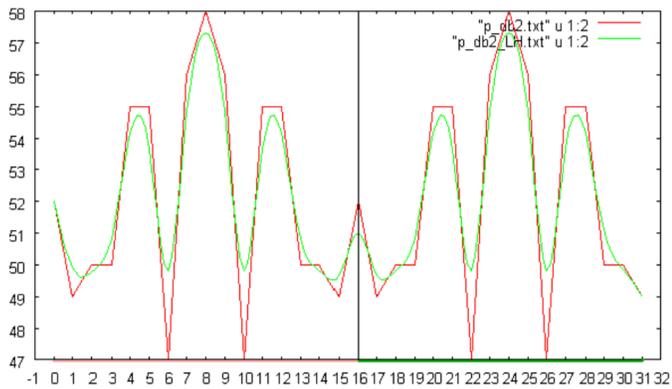


(b)Vertical

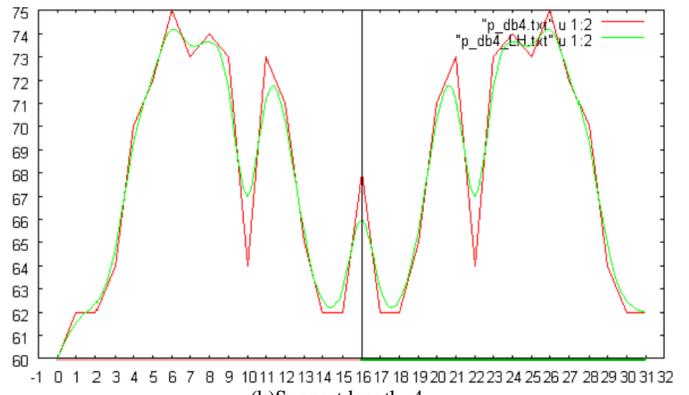


(c)Horizontal

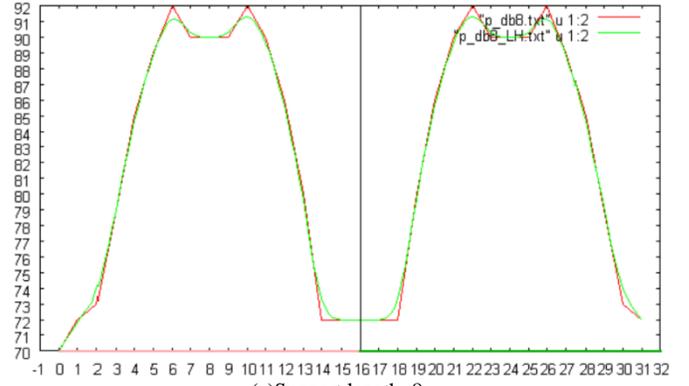
Figure 7 the number of changed pixels in the directions of slant, vertical, and horizontal. In this case, shuttlecock rotates from 0 to 360 degrees in pitch direction. The changed pixels are extracted based on the wavelet transformation with the Daubechies base function of support length of 8.



(a)Support length=2

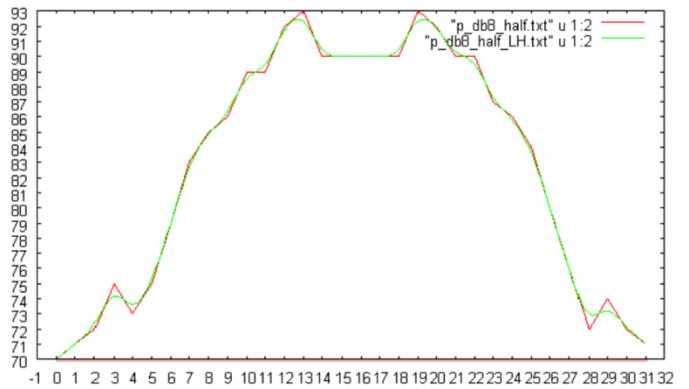


(b)Support length=4

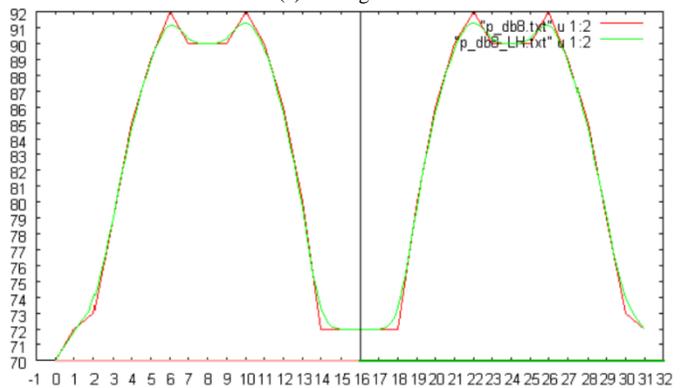


(c)Support length=8

Figure 8 The number of changed pixels for the support length of 2, 4, and 8



(a)180 degree



(b)360 degree

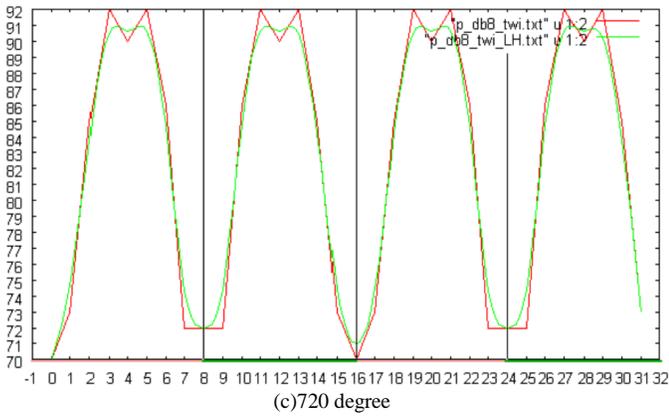


Figure 9 The number of changed pixels when the shuttlecock is rotated by 180, 360, and 720 degrees

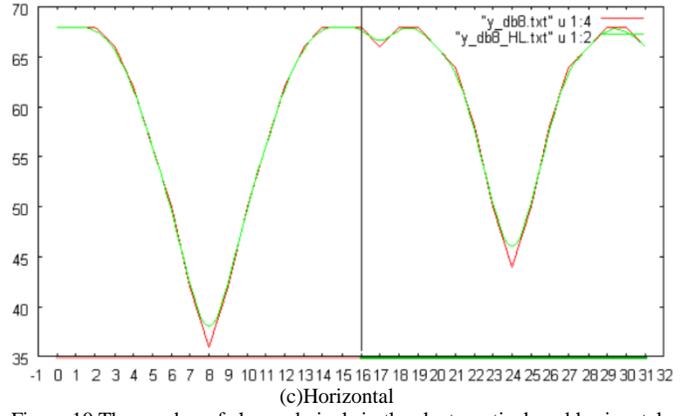


Figure 10 The number of changed pixels in the slant, vertical, and horizontal directions, respectively, which are extracted based on the wavelet transformation with Daubechies base function of the support length of 8. In this case, the shuttlecock is rotated in pitch direction by 360 degrees.

Figure 10 (a), (b), and (c) shows the number of changed pixels in the slant, vertical, and horizontal directions, respectively, which are extracted based on the wavelet transformation with Daubechies base function of the support length of 8. In this case, the shuttlecock is rotated in pitch direction by 360 degrees. Meanwhile, Figure 11 (a), (b), and (c) shows the number of changed pixels in the horizontal direction which are extracted based on the wavelet transformation with Daubechies base function of the support length of 2, 4, and 8, respectively. In this case, the shuttlecock is rotated in pitch direction by 360 degrees.

Figure 12 (a), (b), and (c) shows the number of changed pixels in horizontal direction, when the shuttlecock is rotated by 180, 360, and 720 degrees, respectively.

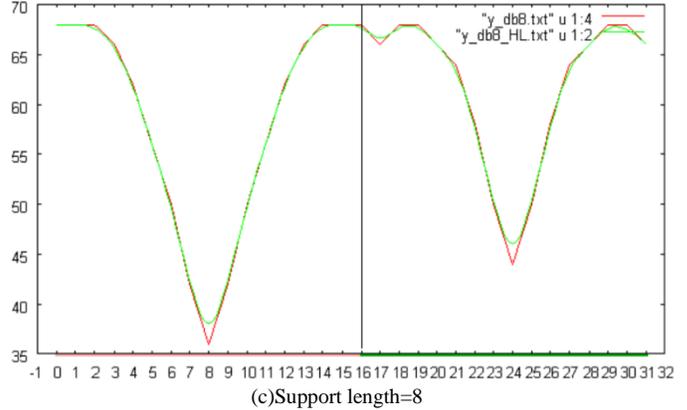
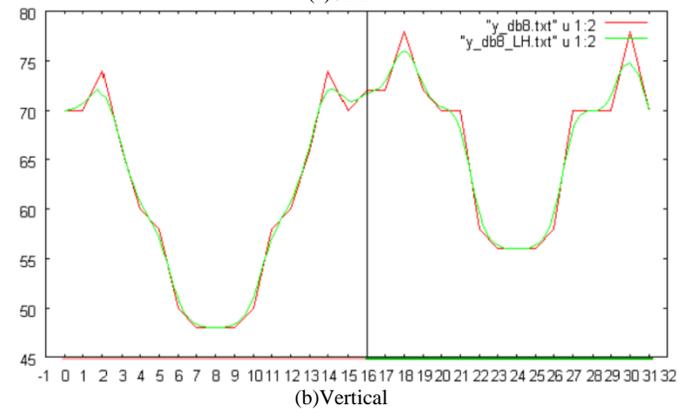
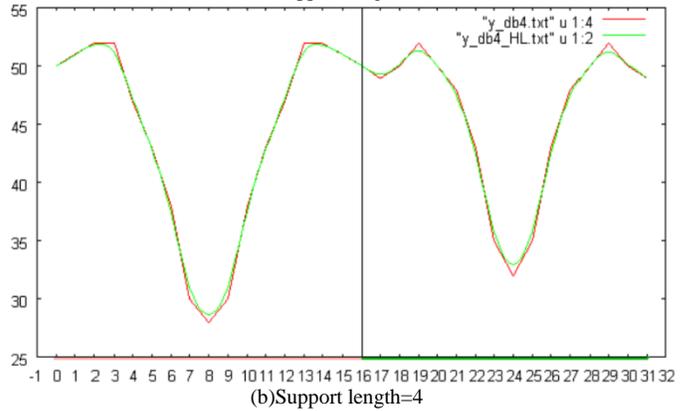
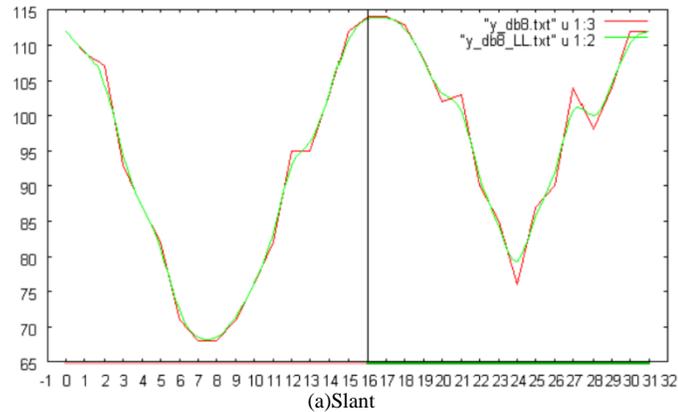
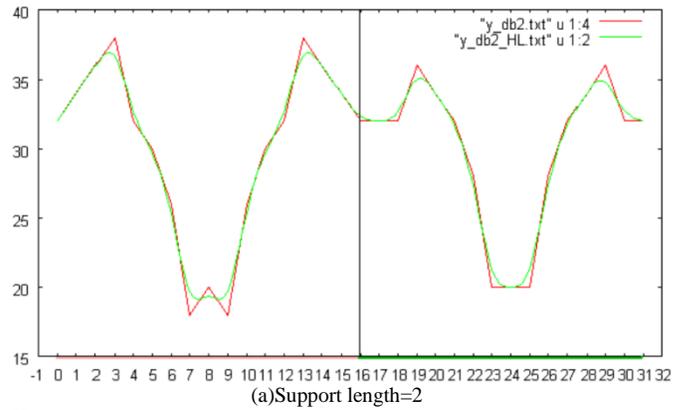


Figure 11 The number of changed pixels in the horizontal direction which are extracted based on the wavelet transformation with Daubechies base function of the support length of 2, 4, and 8, respectively. In this case, the shuttlecock is rotated in pitch direction by 360 degrees.

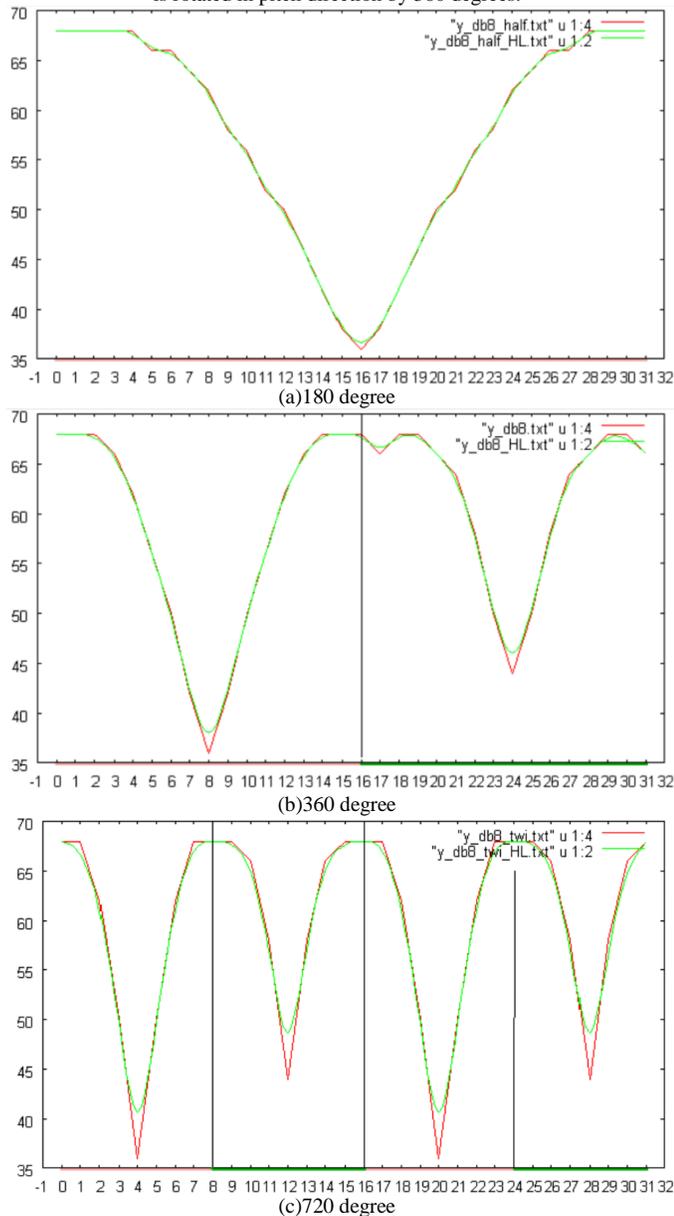
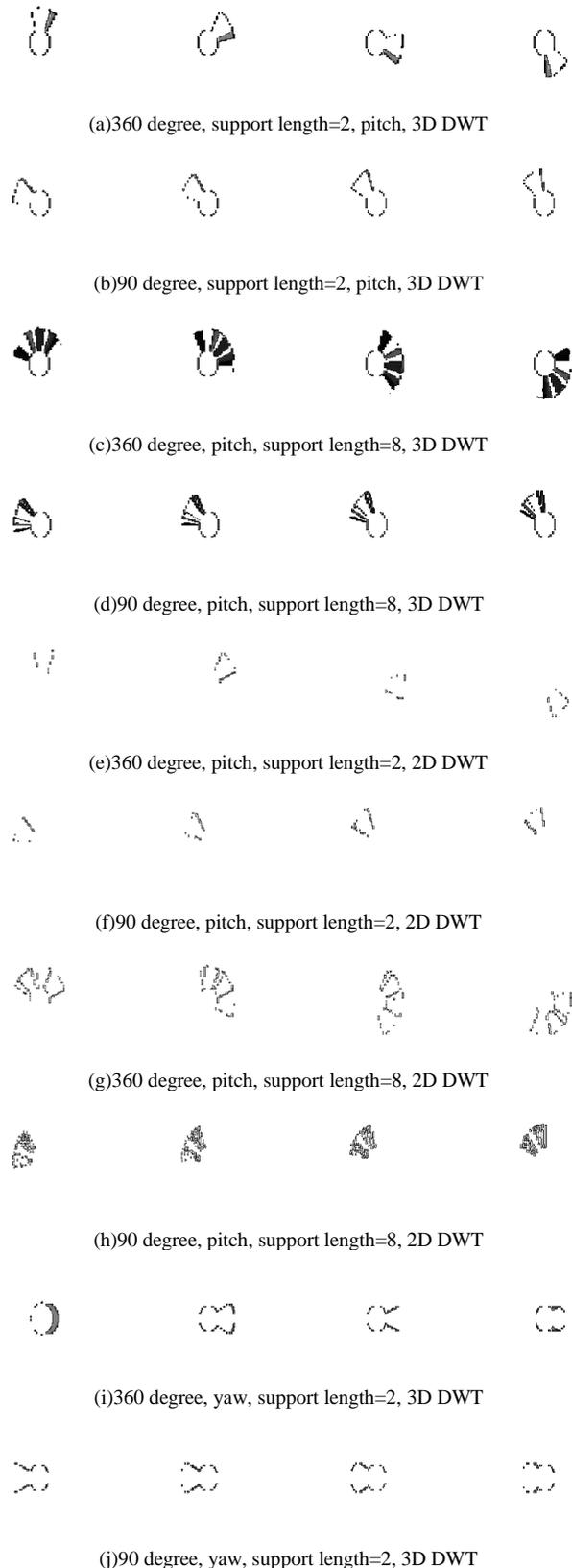


Figure 12 The number of changed pixels in horizontal direction, when the shuttlecock is rotated by 180, 360, and 720 degrees, respectively.

Figure 13 shows the edge enhanced images by 2D and 3D Discrete Wavelet Transformation: DWT with Daunechies base function of support length of 2 and 8 when the shuttlecock rotated in pitch and yaw angles with 90 and 360 degrees.

In general, the number of edge, or changed pixels extracted by 2D DWT is less than that by 3D DWT. Therefore, 3D DWT is much effective than 2D DWT. Also the number of edge, or changed pixels by DWT with support length of 2 is less than that with support length of 8. Therefore, DWT with support length of 2 is effective to extract edge, or changed pixels for the object which moves fast while DWT with support length of 8 is effective to extract edge, or changed pixels for the object

which moves slowly. The terminology of fast and slowly implies the moving speed of the object referencing to the frame rate.





(k)360 degree, yaw, support length=8, 3D DWT



(l)90 degree, yaw, support length=8, 3D DWT



(m)360 degree, yaw, support length=2, 2D DWT



(n)90 degree, yaw, support length=2, 2D DWT



(o)360 degree, yaw, support length=8, 2D DWT



(p)90 degree, yaw, support length=8, 2D DWT

Figure 13 Edge enhanced images by 2D and 3D Discrete Wavelet Transformation: DWT with Daubechies base function of support length of 2 and 8 when the shuttlecock rotated in pitch and yaw angles with 90 and 360 degrees.

IV. CONCLUSION

Method for object motion characteristic estimation based on wavelet Multi-Resolution Analysis: MRA is proposed. With moving pictures, the motion characteristics, direction of translation, roll/pitch/yaw rotations can be estimated by MRA with an appropriate support length of the base function of wavelet. Through simulation study, method for determination of the appropriate support length of Daubechies base function is clarified. Also it is found that the proposed method for object motion characteristics estimation is validated.

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REFERENCES

- [1] K. Arai K. et al., Takagi and Shimoda ed., Image Analysis Handbook, Tokyo Daigaku Shuppan-kai publishing (1991).
- [2] K. Arai K., Fundamental theory for image processing, Gakujutsu-Tosho Shuppan Publishing Co., Ltd (1996).
- [3] K. Arai K., Methods for Image Processing and Analysis of Earth Observation Satellite Imagery Data, Morikita Shuppan Publishing Co., Ltd (1998).
- [4] K. Arai and L. Jameson, Earth observation satellite data analysis based on wavelet analysis, Morikita-Shuppan Publishing Co., Ltd (2001).
- [5] K. Arai K., Java based Earth observation satellite imagery data processing and analysis, Morikita-Shuppan Publishing Co., Ltd (2002).
- [6] K. Arai, K.Seto, Dynamic characteristic identification of moving objects based on wavelet analysis, Journal of Visualization Society of Japan, 24, Suppl.1, 227-230 (2004)
- [7] K.Arai, K.Seto, T. Nishikawa, Method for dynamic characteristic identification of rotated accelerated object based on wavelet analysis, Journal of Visualization Society of Japan, 26, Suppl.1, 145-148, 2006
- [8] K.Arai, T. Nishikawa, Dangerous car identification based on wavelet analysis, Journal of Visualization Society of Japan, 27, Suppl.1, 217-220, 2007
- [9] K.Arai, T.Nishikawa, Identification method for moving object in remote sensing satellite images based on wavelet analysis, Journal of Visualization Society of Japan, 29, Suppl.1, 163-166, 2009.
- [10] K.Arai, T.Nishikawa, Method for optimum support length determinations of Daubechies base function of wavelet in moving object detection of remote sensing satellite images, Journal of Visualization Society of Japan, Journal of Japan Society of Photogrammetry and Remote Sensing, 48, 3, 171-179, 2009.
- [11] K.Arai, Yuji Yamada, Method for determination of optimum support length of base function of wavelet for change detection, Journal of Visualization Society of Japan, 29, Suppl.2,83-86, 2009
- [12] K.Arai, Yuji Yamada, Analysis method for 3D object moments based on wavelet analysis. Journal of Visualization Society of Japan, 30,Suppl.2,287-288,2010

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