Design of ANFIS Estimator of Permanent Magnet Brushless DC Motor Position for PV Pumping System

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Abstract—This paper presents a new scheme for PMBLDC (permanent magnet brushless direct current) rotor position estimation based on an ANFIS (adaptive network fuzzy inference system) estimator. The operation of such motor requires accurate rotor position knowledge. However, most of rotor position sensors produce undesirable effects such as mechanical losses and have other disadvantages. In order to overcome the disadvantages, sensorless scheme seems to offer great advantages. This work presents an ANFIS estimator design. Combining the adaptive capability of the neural network to gather with the reasoning ability of the fuzzy logic in ANFIS modeling results in a fast responding and flexible model. This procedure lends itself perfectly adapted for complex system such as PV pumping systems.

Keywords—Photovoltaic system; Brushless DC motor; ANFIS estimator; Speed controller

I. INTRODUCTION

In early1980s, DC motors are widely used for PV pumping applications either with or without intermediate converters [1]. Starting, steady state, and transient performances of solar power fed DC motors for linear and centrifugal pump load torques were analyzed and showed a perfect matching [2]. However these motors a bulky, and require frequent maintenance. Nowadays solar power fed permanent magnet brushless DC (PMBLDC) motors were being used instead [2].

PMBLDC machine is more popular due its simple structure and low cost [1, 3]. These machines have the advantages of light weight, small size, simple mechanical construction, easy maintenance, good reliability, and high efficiency [1, 3, 4, 5]. In general, the motors are equipped with mechanical position detecting devices to provide proper commutation for power devices in the bridge inverter [6]. These mechanical devices, such as Hall Effect sensor, optical or inductive sensor produce undesirable effects such as mechanical losses and also have other disadvantages like change in mechanical design and requirement of maintenance.

In order to overcome these drawbacks, there is a need to develop a sensorless scheme for estimating rotor position.

In recent years, many sensorless drive methods have been proposed. Of these, the most popular one in the back emf based Filter (EKF) is used [7]. This method provides excellent speed response but requires heavy online matrix computing. An offline FEM assisted position and speed observer has also been studied in the literature [8]. Zero crossing of line to line PM flux linkage is used for estimating the speed and position [9]. Flux Linkage Observer (FLO) based on the integration of back EMF, with a simple start-up method is proposed [10].

In this paper the design of an ANFIS estimator of permanent magnet brushless DC motor in PV pumping system is presented. The Adaptive Neuro Fuzzy Inference System (ANFIS), is a neural network that is functionally the same as a Takagi–Sugeno type inference model. The ANFIS is a hybrid intelligent system that takes advantages of both ANN and fuzzy logic theory in a single system, by using the ANN technique to update the Takagi–Sugeno type inference model parameters. In order to explain the concept of ANFIS structure, five distinct layers are used. The first layer in the ANFIS structure is the fuzzification layer; the second layer performs the rule base layer; the third layer performs the normalisation of membership functions (MFs); the fourth and fifth layers are the defuzzification and summation layer respectively [11].

This rest of the paper is organized as follows. In section 2, the configuration of PV pumping systems is presented. The Adaptive network fuzzy inference system estimator is described in section 3. Section 4 shows the experimental performance of Adaptive network fuzzy inference system estimator. Finally, Section 5 concludes our contribution and merits of this work.

II. GENERAL SYSTEM LAYOUT

The full system mainly consists of the solar cell array generator, DC/DC converter with MPPT (maximum power point tracker) command, PMBLDC motor with its bridge inverter coupled to a centrifugal pump load. The motor is controlled through a hysteresis current loop and an outer speed with PI type controller as shown in fig1.
Fig. 1. Overall system configuration

A. PV generator model

The characteristic of the Photovoltaic generator can be presented by the following nonlinear equation [4]:

\[ I = I_{sc} - I_o \exp\left(\frac{V + RI}{V_{th}}\right) - I_o - \frac{(V + RI)}{R_{sh}} \]  

(1)

Where:
- \( I_{PV} \) Array output current,
- \( R_{sh} \) PV array equivalent shunt resistance,
- \( I_{sc} \) PV array short circuit current,
- \( I_o \) PV array reverse saturation current,
- \( R_s \) PV array series resistance,
- \( V_{th} \) PV array thermal voltage.

The thermal voltage \( V_{th} \) and reverse saturation current \( I_o \) are successively identified by [4]:

\[ V_{th} = \frac{V_{op} + R_s I_{op} - V_{sc}}{\log\left(1 - \frac{I_{op}}{I_{sc}}\right)} \]  

(2)

\[ I_o = (I_{sc} - I_{op}) \exp\left(-\frac{(V_{op} + R_s I_{op})}{V_{th}}\right) \]  

(3)

B. Permanent magnet Brush-Less DC motor model

The simplified schematic of PMBLDC motor who has a trapezoidal electromotive force, the use of Park transform is not the best approach in modelling the machine. Instead the natural approach is used where the emf is generated with respect to rotor position [4]. The operating sequences of the machine can be subdivided into six cycles with respect to rotor position as shown in II.

The electric of the motor can be described by [4]

\[ V_{an} = R_i a + p l_a + e_a \]  

(4)

\[ V_{bn} = R_i b + p l_b + e_b \]  

(5)

\[ V_{cn} = R_i c + p l_c + e_c \]  

(6)

With

\[ V_{an} = V_{a0} - V_{n0} \]  

(7)

\[ V_{bn} = V_{b0} - V_{n0} \]  

(8)

\[ V_{cn} = V_{c0} + V_{n0} \]  

(9)

Where \( R \): per phase stator resistance. \( i_{a,b,c} \) and \( \lambda_{a,b,c} \) are respectively phase currents of phases a, b and c and total flux linkage of a, b and c. p: Laplace operator.

The flux expressions are given by the following expressions:

\[ \lambda_a = L_s i_a - M(i_b + i_c) \]  

(10)

\[ \lambda_b = L_s i_b - M(i_a + i_c) \]  

(11)

\[ \lambda_c = L_s i_c - M(i_a + i_b) \]  

(12)

Where \( L_s \): the self-inductance and \( M \): the mutual inductance.

And

\[ i_a + i_b + i_c = 0 \]  

(13)

Therefore by substituting Eq.13 in Eqs 10, 11 and 12:

\[ \lambda_a = i_a (L_s + M) \]  

(14)

\[ \lambda_b = i_b (L_s + M) \]  

(15)

\[ \lambda_c = i_c (L_s + M) \]  

(16)

From the electrical equations 4, 5 and 6, the following system is obtained

\[ \begin{bmatrix} V_{an} \\ V_{bn} \\ V_{cn} \end{bmatrix} = \begin{bmatrix} R & 0 & 0 \\ 0 & R & 0 \\ 0 & 0 & R \end{bmatrix} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} L_{eq} & 0 & 0 \\ 0 & L_{eq} & 0 \\ 0 & 0 & L_{eq} \end{bmatrix} \begin{bmatrix} l_a \\ l_b \\ l_c \end{bmatrix} + \begin{bmatrix} e_a \\ e_b \\ e_c \end{bmatrix} \]  

(17)

With \( L_{eq} = L_s - M \)

From this system, the decoupled phase equations are obtained and the explicit current equations are given by:
The mechanical part is expressed by the following equation:

\[
\frac{1}{J} \frac{d\omega}{dt} + B\omega = T_e - T_r
\]

With:

- \( T_e \): electromagnetic torque.
- \( T_r \): Load torque
- \( \Omega \): speed
- \( J \): moment of inertia
- \( B \): viscous friction coefficient

Neglecting the frictional coefficient and taking \( \Omega = \frac{\omega}{P} \) where \( P \) is the pole pairs number, (19) can written as:

\[
\frac{d\omega}{dt} = P. (T_e - T_r) / J
\]

The developed torque can be expressed by

\[
T_e = (e_a i_a + e_b i_b + e_c i_c) / \omega
\]

And the angular position is expressed by

\[
\frac{d\theta}{dt} = \omega
\]

C. Speed control

PI speed controller is widely used in industry due to its ease in design and simple structure. The rotor speed \( \omega(k) \) is compared with the reference speed \( \omega_{ref}(k) \) and the resulting error is estimated at the \( n^\text{th} \) sampling instant as:

\[
e(k) = \omega_{ref}(k) - \omega(k)
\]

\[
\Delta e(k) = e(k) - e(k - 1)
\]

The value of the torque reference is given by [4]:

\[
T_{ref}(k) = T_{ref}(k - 1) + K_p \Delta e(k) + K_i e(k)
\]

Where \( e(k - 1) \), the speed error of previous interval is, \( e(k) \) is the speed error of working interval. \( k_p \) and \( k_i \) are speed controller gains.

D. Current control

Several techniques can be used to control the phase current of the PMBLDC motor. In this paper a hysteresis current controller is used. It has the major advantage of not requiring machine parameters to be known. However the commutation frequency is not constant [4]. It depends on many factors such as the applied voltage, the back emf, hysteresis band \( \Delta I \)...etc.

Maximum value of commutation frequency is obtained at starting and is given by [4]:

\[
F_{max} = \frac{U}{8L_5 \Delta I}
\]

The commutations are obtained by comparing actual currents \( i_{a,b,c} \) to a rectangular reference \( i_{a,b,c}^* \) and by keeping them in hysteresis band \( \Delta I \). The commutation sequences of switches are summarised in the table I. [5].

<table>
<thead>
<tr>
<th>TABLE I. THE COMMUTATION SEQUENCES OF SWITCHES</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_a )</td>
</tr>
<tr>
<td>( i_a &lt; (i_a^* - \Delta I) )</td>
</tr>
<tr>
<td>( i_a &gt; (i_a^* + \Delta I) )</td>
</tr>
<tr>
<td>( i_b &lt; (i_b^* - \Delta I) )</td>
</tr>
<tr>
<td>( i_b &gt; (i_b^* + \Delta I) )</td>
</tr>
<tr>
<td>( i_c &lt; (i_c^* - \Delta I) )</td>
</tr>
<tr>
<td>( i_c &gt; (i_c^* + \Delta I) )</td>
</tr>
</tbody>
</table>

E. Pump model

A centrifugal type is used. It can be described as an aerodynamic load which is characterised by the following load equation [4]:

\[
T_1 = A.\omega^2
\]

Where \( A \) is the pump constant.
TABLE II. OPERATING SEQUENCES WITH RESPECT TO ROTOR POSITION

<table>
<thead>
<tr>
<th>Rotor position</th>
<th>Phase voltages, back emf and reference current values</th>
</tr>
</thead>
<tbody>
<tr>
<td>θ°</td>
<td>V_{as}</td>
</tr>
<tr>
<td>0°-60°</td>
<td>U/2</td>
</tr>
<tr>
<td>60°-120°</td>
<td>U/2</td>
</tr>
<tr>
<td>120°-180°</td>
<td>0</td>
</tr>
<tr>
<td>180°-240°</td>
<td>U/2</td>
</tr>
<tr>
<td>240°-300°</td>
<td>U/2</td>
</tr>
<tr>
<td>300°-360°</td>
<td>0</td>
</tr>
</tbody>
</table>

III. ANFIS ESTIMATOR

The adaptive network fuzzy inference system plays a significant role in the field of artificial intelligence. It combines the advantages of a fuzzy controller as well as quick response and adaptability nature of artificial neural network [11]. Hence using this scheme one can avoid the use of a position sensor which produces mechanical losses in the motor. Different configurations of adaptive network fuzzy inference system have been tested and the best one that gives the minimum error value is presented in fig. 6.

The Algorithm of the model structure was constructed as shown in Fig.3. The membership functions were obtained from the data set of the back emfs which were first normalized for loading data. Then generate Fis, built on sugeno structure, which is obtained by creating of input membership function: number (tree inputs) & type (triangular) and output type(linear). The choice of optimization method (hybrid) is obtained by Train Fis. If the results are satisfactory (error is minimum) after test Fis, denormalized procedure is done and go to application thereafter. The ANFIS structure consists of 5 layers of neurons, each of which having a very specific behavior.

From these, second, third and fifth layer have constant behavior, while layers 1 and 4 have varying parameters.

**Layer 1**: consists of five adaptive neurons in which the fuzzification is performed, that is: the grade of membership to the defined membership functions of the input is evaluated.

\[ f_i^1 = \mu_{A_i}(x) \]  

(28)

Where \( x \) is the input to \( i^{th} \) neurons and \( A_i \) is membership function correspond to variable \( x \).

The membership function \( \mu_{A_i}(x) \) is triangular.

**Layer 2**: consists of 125 neurons, each node output represents the firing weight of a rule gives than:

\[ W_k = \mu_{A_i}(x) \times \mu_{B_j}(y) \]  

(29)

\( k \) : represent the number of rule, \( i \) : represent the number of \( x \) partition and \( j \) : number of \( y \) partition.

Fig. 3. Algorithm of the ANFIS model

**Layer 3**: consists of 125 neurons, every node calculates the ratio of every rule firing weight to the sum of all rule firing weights.

\[ \overline{W_k} = \frac{W_k}{\sum W_i} \]  

(30)
Layer 4: consists of 125 neurons. Nodes in layer 4 are adaptive nodes in which the consequent evaluation inference is calculated, its output is defined as:

\[
f_k^4 = \overline{W_k} \times f_k = \overline{W_k} \times (p_k x + q_k y + r_k) \quad (31)
\]

\(\overline{W_k}\) is the output of layer 3 and \(\{p_k, q_k, r_k\}\) is called consequent parameters.

Layer 5: Finally, is single node in layer 5, where sums all the outputs from 4th layer to compute the overall output of the network:

\[
f^5 = \sum \overline{W_k} \times f_k^4 \quad (32)
\]

IV. SIMULATION RESULTS

The entire ANFIS network architecture is represented in the Fig.6. The inputs are the three line to line back emfs of the motor namely Eab, Ebc and Eca Fig.4. And the desired output is the estimated rotor position angle. For producing the above relationship with least possible error, a five layer feed forward adaptive network fuzzy inference system is used. The input layer consists of five neurons that have their inputs as the three line to line back emfs, the three hidden layers consists of 125 each and the output layer consists of a single neuron whose output is the estimated position of the rotor. The relationship between the back emf and the position of the rotor is shown in the Fig.5.

Fig.7 shows estimated rotor position by adaptative network fuzzy inference system and the error, along with real rotor position it’s a case without regulation. Fig.8 shows the estimated rotor position by adaptive network fuzzy inference system and the error, along with real rotor position the case is with PI speed control. In the comparison of the cases with control (PI regulator) and at without control. The controlled system attains the steady state in (0.04s) greater than the case without regulation the system attains the steady state in (0.023s), so the PI regulator slows the dynamic responses.

The performance of the trained adaptive network fuzzy inference system is found to have very minimal errors which is about 1.303e-7 as seen in the Fig.7 (without control).

![Fig. 7. The inputs curves](image)

![Fig. 6. Structure of ANFIS model proposed](image)

For Fig.8 (with PI controller), the error is 7.8386e-9. The error of output of ANFIS and real rotor position sensor are compared through Fig.7 and Fig.8 respectively. It is clear that the error in Fig.8 is too small (7.8386e-9) than these in Fig.7 (1.303e-7). The proposed scheme works efficiently where the usage of neural network topology together with fuzzy logic in the adaptive network, ANFIS, not only includes the characteristics of both methods, but also eliminates some disadvantages of their lonely-used case.

![Fig. 5. The back emf Eab](image)

![Fig. 6. Structure of ANFIS model proposed](image)
Fig. 7. Simulation Results without control

Fig. 8. Simulation Results with PI controller

V. CONCLUSION

The developed ANFIS models were successful in estimating rotor position of PMBLDC motor used in PV pumping system. In this paper the design of adaptive network fuzzy inference system based sensorless scheme was developed for permanent magnet brushless DC motor. The proposed scheme works efficiently for both with control (PI regulator) and at without control. It was found that the error is very minimal and this is smaller in system with regulation, than these without regulation. Also adaptive network fuzzy inference system based estimator is very flexible. This scheme not only eliminates the position sensor, thereby cutting the cost but also transforms the drive into a highly efficient drive by eliminating losses caused by position sensors. The estimation error is found to be very minimal proving that the developed system is a very efficient and a reliable one.

REFERENCES

The PV generator, motor and pump used in this study have the following parameters: PV generator Modules AEG-40. (Temperature T=25°C and solar insolation E=1000W/m².)

Open circuit voltage 22.40 V
Short circuit current 2.410 A
Series resistance 0.450 Ω
Current temperature coefficient 0.06%/ C
Voltage temperature coefficient 0.40%/ C

Centrifugal pump
- Rated speed 3000 rev/min
- Rated power 521 W
- Flowrate 2.597 l/s
- Head 14.11 m
- Efficiency 69%

Brushless DC motor
- Rated power 690 W
- Rated speed 3000 rev/min
- Rated voltage 200-220V
- Rated current 4.8 A
- Per phase resistance 1Ω
- Per phase inductance 5 mH
- Poles number 6
- E.m.f constant 0.47