Light but Effective Encryption Technique based on Dynamic Substitution and Effective Masking

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Abstract—Cryptography and cryptanalysis are in ever-lasting struggle. As the encryption techniques advance, the cryptanalysis techniques advance as well. To properly face the great danger of the cryptanalysis techniques, we should diligently look for more effective encryption techniques. These techniques must properly handle any weaknesses that may be exploited by hacking tools. We address this problem by proposing an innovative encryption technique. Our technique has unique features that make it different from the other standard encryption methods. Our method advocates the use of dynamic substitution and tricky manipulation operations that introduce tremendous confusion and diffusion to ciphertext. All this is augmented with an effective key expansion that not only allows for implicit embedment of the key in all of the encryption steps but also produces very different versions of this key. Experiments with our proof-of-concept prototype showed that our method is effective and passes very important security tests.

Keywords—Encryption techniques; dynamic substitution; key expansion; directive based manipulation; block masking

I. INTRODUCTION

In the digital era, almost all of our sensitive information is either transmitted over the network or digitally stored on machines. This information will inevitably be in a great risk if we do not properly secure them. Encryption is the de-facto means for keeping the security of the transmitted or stored information. Many encryption techniques have been proposed (e.g. [1][2][3][4][5][6][7][8][9][10][11][12][13][14][15][16][17][18]). Although these methods are effective and purport to provide high levels of security, there is always a truly pressing need for new techniques that can effectively and properly handle any weaknesses that may be exploited by hacking tools.

This paper proposes an effective encryption technique. This technique consists of three effective encryption operations along with a novel key expansion operation. First, the proposed substitution operation adopts dynamic behavior. Unlike all other encryption techniques (noticeably [3]), which use a static substitution operation, our technique uses a dynamic substitution operation whose state depends on the key and greatly sensitive to its changes. Second, the diffuse operation is highly sensitive to changes of the key or the plaintext block and is capable of greatly magnifying and then propagating these changes to all of the block’s symbols. Third, the masking operation uses a novel technique that makes sharp changes to both the individual symbols of the plaintext block and to its structure. Finally, the key expansion technique proposes an innovative model that combines the lookback-based substitution with the random manipulations.

The paper makes the following contributions. First, it proposes a full-fledged encryption technique. Second, it proposes an effective dynamic substitution operation whose functionality highly depends on the key. Third, it proposes a novel key expansion technique. Forth, it proposes an effective masking operation that impacts both the block’s individual symbols and the structure of the block.

We present our contribution as follows. Section II describes the technical details of the dynamic substitution operation. Sections III through VI present the details of the operations that comprise our proposed cipher. Section VII presents the technical details of the proposed cipher. Section VIII presents the related work. Section IX presents the performance analysis of our technique. We conclude and give directions for future work in Section X.

II. DYNAMIC BOX SUBSTITUTION

The purpose of the substitution is to move from the actual block symbols to new symbols. It uses a data structure superficially similar to S–Box of AES encryption method [3], but is fundamentally different in its dependency on the key. This section describes the D–Box and discusses how it is used in substituting symbols.

A. The D-Box and its Inverse D-Box

The D-Box is conceptually $K \times K$ array. The D-Box is populated with the unicode symbols from 0 to $K^2-1$. Each symbol in the D-Box can be accessed by its column and row indexes. The positions of the unicode symbols in the D-Box are never static. Their locations depend on the encryption key. To do this, we utilize a sequence of integers $I_1I_2...I_m$, which are generated in a process that involves the key. (The process for generating these integers is discussed in Appendix A.) These integers are used to reposition the symbols in the D-Box. The repositioning of the symbols is performed by swapping the symbol at the index $i$ in the D-Box with the symbol at the index $I_i$.

In order to use the D-Box for encryption, it is necessary to define the inverse substitution so that the original block can be recovered. Fig. 1 illustrates the process of creating D-Box$^{-1}$ from the D-Box. Given a $16 \times 16$ D-Box, the D-Box$^{-1}$ is created as follows. For each symbol $s$ in D-Box[$r$, $c$], we create an entry in the D-Box$^{-1}$ by dividing the 8 bits of $s$ into two sets and replacing each set with the index $I_s$.
B. Symbol-Substitution using D-Box / D-Box−1

We define two substitution operations. The first operation is called Substitute, which uses the D-Box for replacing a symbol $p$ with a new one. The second operation is called Inverse Substitute, which replaces a symbol $q$ using D-Box−1. Substituting a symbol using the D-Box and D-Box−1 is straightforward. It is a table lookup operation. Given a symbol $p$, the left half bits of $p$’s binary representation index the row of the D-Box and the right half bits index its column. Indexing D-Box−1 is done in an identical way.

Fig. 2 shows an example of D-Box and its Inverse D-Box−1 (right). For the sake of the simplicity, we use only the hexadecimal numbers. Since we have only 16 symbols, our D-Box is $4 \times 4$. Therefore, we need two bits to index its rows and two bits to index its columns. The two bits at the top index the column and the two bits on the leftmost index the rows.

To illustrate the substitution operation, consider a block of four symbols “9C06”. The Substitute operation reads the first symbol “9” whose binary representation is “1001”. The left two bits “10” index the row of the D-Box and the right two bits “01” index the column. The symbol at row 2 (“10”) and column 1 (“01”) in the D-Box is retrieved as a substitute for the symbol “9”. Thus, the symbol “9” is substituted with “7”.

Continuing likewise, the entire block is substituted yielding the new block “7F4B”.

To recover the original block from “7F4B”, we use the Inverse Substitute operation. The binary of the symbol “7” is “0111”. The left half bits “01” index the row of the D-Box−1 and the right half bits “11” index its column. As a result, the symbol at row 1 and column 3, which is “9”, is retrieved from the D-Box−1. The next symbol is “F” whose binary representation is “1111”. Thus, the symbol at row “11” and column “11”, which is “C”, is retrieved from the D-Box−1. Using the same process, we recover the original block “9C06”.

III. Key Expansion

The key expansion process expands encryption keys to an arbitrary length. The process defines two operations. The first one is the substitution operation whose logic is fully described by Fig. 3. The input to this operation is a key, which consists of $n$ unicode symbols $k_1k_2...k_n$. The output is a new (substituted) key $W$ whose length is also $n$ symbols. As the logic clearly shows, the first symbol $k_1$ in the key is substituted with a new one using the D-Box. For all the symbols $k_i$ ($i=2, 3, ..., n$), the operation uses the outcome of substituting $k_{i-1}$ (or $T_{i-1}$) to substitute the symbol $k_i$. Therefore, to create a new symbol in the output key $W$, the operation XORs the current symbol of the input key $k_i$ and the result of the previous substitution $T_{i-1}$ to create a new symbol $K_i^*$. The symbol $K_i^*$ is substituted to produce the new symbol $T_i$ in the output key.

The second operation, called Manipulate, creates sharp modifications to its input string. The modifications include changes to both individual symbols and the structure of the input string. Suppose $t_1t_2...t_n$ be an input string. The manip-
\[
\text{Manipulate}(t_i) = \begin{cases} 
\text{LH} & \text{if } t_i \leq t_{i+1} \\
\text{RH} & \text{if } t_i > t_{i+1}
\end{cases}
\]

Fig. 4. the manipulation operation.

\[
\gamma \leftarrow \text{uniform Random} \quad (0, 1)
\]

Yes\quad \text{execute} \text{Flip}(t_i)\quad \gamma \leq \text{LTE} \\
No\quad \text{execute} \text{FlipSwap}(t_i)
\]

Fig. 5. the dynamic random model for action selection.

The manipulate operation handles each symbol \( t_i \) using the two actions defined in Fig. 4.

The manipulate operation (Fig. 4) handles each symbol \( t_i \) based on the lookahead symbol \( t_{i+1} \). If symbol \( t_i \) lexically comes before or equal to the lookahead symbol \( t_{i+1} \), the left half bits of \( t_i \) are flipped using the action \( L_{\text{Flip}}(t_i) \). If otherwise, the right half bits of \( t_i \) are flipped and the resulting symbol is moved to a position determined by the lookahead symbol \( t_{i+1} \). Consider for instance the input string “pcestreeeeloop”. If the current symbol is “p”, then the left half bit of “p” \((01110000)\) are flipped because “p” lexically comes before the lookahead symbol “q” yielding “q” \((10000000)\). Assume that the current symbol is “q”. The lookahead symbol is thus “e”. Since “q” lexically comes after “e”, the right half bits of “q” \((01110001)\) are flipped \((01111110)\) yielding “~e”. Additionally and based on Fig. 4, the resulting symbol “~e” is moved to the position \( 101 \% 12 = 5 \) in the string. \((101 \text{ is the Unicode index of the lookahead symbol “e” and 12 is the length of the input string})\) This operation results in “~e...~......”.

Although selecting and applying one of the two actions of the Manipulate operation based on the lexical order of input symbols may be effective by itself, we prefer to add more randomness to the action selection. As such, instead of using the plain lexical order of the input symbols, we introduce a random noise to the action selection. In particular, we define a dynamic random model that guides the selection process (Fig. 5). Let \( T \) be the number of the so-far processed symbols and \( P \) be the number of times in which \( t_i \leq t_{i+1} \). Based on this, we define two dynamically updated variables \( \text{LTE} \) and \( \text{GT} \) as follows.

\[
\text{LTE} = \frac{P}{T} \quad \text{and} \quad \text{GT} = 1 - \frac{P}{T}
\]

Where \( \text{LTE} \) means “less than or equal” and represents the ratio in which the condition \( t_i \leq t_{i+1} \) holds. \( \text{GT} \) means “greater than” and represents the ratio in which the condition \( t_i \leq t_{i+1} \) is false. Using these two variables, we redefine our Manipulate operation (Fig. 4) in Fig. 5.

Although neither \( \text{LTE} \) nor \( \text{GT} \) is random, their values change (increase or decrease) based on the lexical order of the current symbols \( b_i \) and the lookahead symbols \( b_{i+1} \). The amount of the bias toward either action therefore does change. When \( \text{LTE} \) increases \((\text{GT} \) decreases\), the likelihood of executing the \text{Flip} action becomes larger than the likelihood of executing \text{FlipSwap} action. Likewise, when \( \text{GT} \) increases \((\text{LTE} \) decreases\), the likelihood of executing the \text{FlipSwap} action becomes larger than that of executing \text{Flip} action. As such, \( \text{LTE} \) increases \((\text{or decreases})\) the likelihood of the executing an action over the other, but the choice of the action to be executed happens randomly since it depends on the random value \( \gamma \).

After introducing the two operations that constitute the key expansion process, we delineate this process in Fig. 6. The logic is straightforward. We start with the input key \( k_1k_2...k_n \). The process creates a new version of the input key using the steps 1 through 7. The symbols of the input key are first substituted with new symbols \( x_i \)’s. Next, the new symbols \( x_i \)’s are manipulated using the manipulation operation (Fig. 5). To define the amount of the bias \( \text{LTE} \) (line 6), we always increment the number of processed symbols \( T \) while incrementing \( P \) only when the currently processed symbols \( x_i \) lexically equals to or comes before the lookahead symbols \( x_{i+1} \). Therefore, the ratio \( \text{LTE} \) is always in the interval \([0, 1]\) and represents a likelihood of executing \text{Flip} action.

The new version of the key \( S \) is concatenated with the original key. If the desired length has not been reached yet (step 9), the process uses the latest version \( S \) of the key to create a new version.

IV. DIFFUSE AND INVERSE DIFFUSE OPERATIONS

The diffuse operation detects changes in the input block and propagates this change to affect every symbol in the corresponding output block. To be effective, the diffuse operation must be highly sensitive to the input’s change regardless of its magnitude and amplify it so that this change causes tremendous changes to the output. The inverse diffuse operation reverses the effect of the diffuse operation and recovers the original input.

Fig. 7 shows the algorithmic steps for the diffuse operation. As the figure shows, it performs double substitutions for the
block's symbols: forward and backward substitutions. When operates on an input block \( b_1b_2...b_n \), the forward substitution effectively propagates the change in a symbol \( b_i \) to all the following symbols \( b_j \) \((j > i)\). First, the operation substitutes \( b_1 \) to yield a new symbol \( c_1 \). For every subsequent input symbol \( b_i \) \((i > 1)\), the operation first XORes \( b_i \) with the result of the previous substitution \( c_{i-1} \) and substitutes the outcome of the XOR. That is, the symbol \( t_i \) is calculated as \( t_i = b_i \oplus c_{i-1} \) and then substituted to yield a new symbol \( c_i \).

As Fig. 7 shows, the output of the forward substitution \( c_1c_2...c_n \) is passed to the backward substitution. The backward substitution uses similar logic as the forward except that it starts from the end of the input block. The backward substitution substitutes \( c_n \) to yield the output symbol \( S_n \). For the input symbols \( c_i \) \((i=n-1, n-2, \ldots, 1)\), \( c_1 \) is first XORed with \( S_{i+1} \) and the result of the XOR operation is substituted to yield \( S_i \).

With this feedback-based forward substitution, the result of substituting a symbol \( b_i \) is impacted not only by the symbol \( b_i \) per se, but also by the symbol \( b_{i-1} \). That is because if a symbol \( b_i \) changes so does its substitution outcome. This change also impacts the substitution of the following symbol \( b_{i+1} \) due to the XORing operation, which in turn impacts the substitution of \( b_{i+2} \), and so on. In other words, the change in symbol \( b_i \) collectively creeps to affect all the successive symbols \( b_j \) \((j > i)\). Similarly, the backward substitution propagates the change in the symbol \( b_i \) back to the symbols \( b_k \) \((k < i)\). In this case, no matter where the change occurs, the forward and backward substitutions always guarantee that this change impacts every symbol of the input.

The diffuse operation can be reversed. Fig. 8 shows the algorithmic steps of the inverse diffuse operation. As the figure shows, the operation starts from the backward substitution to recover the original block \( b_1b_2...b_n \). The input to backward substitution is \( S_1S_2...S_n \). The backward operation yields the block \( c_1c_2...c_n \). This block is passed as an input to the forward substitution operation, which recovers the original block.

Table I shows an example of the diffuse operations output. The input blocks in the first three rows differ in only a single bit. This minor change causes a very remarkable difference in the corresponding output blocks. Additionally, the position of the change plays a major role. As an example, compare between the output in row 1 and the second and third rows.

V. Directive Generator

This section describes the directives generator. Subsection V-A discusses the mesh and Subsection V-B shows how to use the mesh to produce directives.

A. The Mesh

Conceptually the mesh is a two dimensional array. The horizontal and vertical dimensions are populated with the unicode symbols from 0 to some integer \( N \). Fig. 9 provides an example of a mesh.

Each cell in the mesh is accessed by its row and column indexes. Each move within the mesh whether along the vertical or horizontal dimension has a distance and a direction with respect to the current position. The distance of the move \( d \) is the number of cells passed. The direction of the move is either toward a lower or a higher index. We capture the move toward the lower indexes by the flag \( "<" \) and toward the higher indexes by the flag \( ">" \) regardless whether this move is along the horizontal or vertical dimension. For example, if we move from the current point, say \( P_1 \), to \( P_2 \), the distance of the move...
is 3 and the direction is captured by “−” because we moved three cells to the lower indexes. As another example, the move from the current point \( P_1 \) to \( P_3 \) has a distance of 2 and the direction is “+” because we moved two cells to the higher indexes.

We can now formally define a directive as a signed integer \( \pm x \), where \( x \geq 0 \) represents the distance of the move and \( \pm \) represents its direction. Accordingly, moving from the current point \( P_1 \) to \( P_2 \) is captured by the directive “−3” and from \( P_1 \) to \( P_3 \) is captured by the directive “+2”.

### B. Mesh-Based Mapping

Based on the mesh and directive definition, the proposed mesh-based mapping consists of two operations: Mapping and Dimension Selection (see Fig. 10). The mapping operation utilizes three inputs: a block of symbols to be mapped \( b_1 b_2 ... b_n \), a mapping dimension \( d_i \) (could be the horizontal or the vertical dimension of the mesh), and a starting point \( (h, v) \). The starting point \( (h, v) \) is a point within the boundary of the mesh and from which the mapping is started; where \( h \) represents the index on the horizontal dimension and \( v \) represents the index on the vertical dimension.

Initially, the starting point is created from the first symbol of the input \( b_i \)'s and the first symbol of the input \( s_i \)'s. That is, the starting point is defined as \((s_1, b_1)\). The mapping operation updates the starting point as the mapping proceeds (after producing each directive). Additionally, for mapping any subsequent block, the latest starting point is used for the mapping.

The dimension selection operation utilizes a sequence of symbols \( s_1 s_2 ... s_n \) and produces a dimension \( d_i \), which can be either one of the two mesh dimensions. The logic of the dimension selection operation must be based on the sequence \( s_i \)'s. For the purpose of this paper, the dimension selection operation uses the following simple functionality: the mapping dimension \( d_i \) is the horizontal if the unicode index of \( s_i \) is odd; otherwise the mapping dimension is the vertical.

Based on this, we can formally define our mapping for a symbol \( b_j \) as follows. First, the dimension selection operation uses its input symbol \( s_i \) to determine the mapping dimension \( d_i \). The mapping operation uses the current value of the starting point and the mapping dimension \( d_i \) to map the symbol \( b_j \) and produce a directive \( \pm x_j \). Specifically, the mapping begins from the starting point and moves along the mapping dimension toward the index of \( b_j \) in this dimension. Both the number of cells passed and the direction with respect to the reference point (starting point) are compiled into a directive “−x” or “+x”, where \( x \) is the distance. The mapping operation updates the starting point to the new position before mapping any new symbol \( b_j \).

Fig. 11 provides an example. Suppose that we want to map the symbol “m” to the mesh. Suppose that the current value of the starting point is \((h = 7, v = 3)\) and the input symbol for the dimension selection operation is “a”. Since the value of the symbol “a” in the unicode coding is 97, which is odd, the mapping dimension is the horizontal dimension. Therefore, the mapping operation starts from the starting point \((7, 3)\) and moves along the horizontal dimension to the index of “m”. Since the number of passed cells is 4 and the direction of the move is to the higher indexes, the mapping yields the directive “+4” as a result of the mapping. The mapping operation produces accordingly the directive “+4” as a result. The starting point is updated to \((7, 7)\). As a final illustration, suppose that we want to map the symbol “e”, where the input of the dimension selection is “a” and the starting point is \((7, 3)\). Since the value of “a” is 97, which is odd, the mapping dimension is the horizontal. The mapping operation hence starts from the starting point \((7, 3)\) and moves along the horizontal dimension to the position of “e”. Since the distance of the move is 5 and is toward the lower indexes, the mapping operation produces the directive “−5” as a result of the mapping. The starting point is updated to \((2, 3)\).

### VI. Mask Process

This mask process deeply alters its input block. The alteration includes (1) masking the symbols and (2) altering both the symbols and the block’s structure. Fig. 12 shows the main operations of the mask process.

First, the mask process executes the ** Manipulate operation**. This operation uses a sequence of the directives “+d_1 +
Fig. 12. The main actions of the mask operation.

<table>
<thead>
<tr>
<th>Current sign</th>
<th>Lookahead sign</th>
<th>Action Performed on the block</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S_i )</td>
<td>( S_{i+1} )</td>
<td></td>
</tr>
<tr>
<td>+</td>
<td>-</td>
<td>LR Crossover: left half bits of the symbol ( b_i ) is exchanged with the left half bits of ( b_{i+1} ).</td>
</tr>
<tr>
<td>+</td>
<td>+</td>
<td>Flip: flip the bits of the current input symbol ( b_i ).</td>
</tr>
<tr>
<td>-</td>
<td>+</td>
<td>RL Crossover: right half bits of the symbol ( b_i ) is exchanged with the right half bits of ( b_{i+1} ).</td>
</tr>
<tr>
<td>-</td>
<td>-</td>
<td>Scatter: move the symbol ( b_i ) ahead ( d_i ) positions, where ( d_i ) is the plain directive.</td>
</tr>
</tbody>
</table>

Fig. 13. The logic of the manipulate operation. The figure demonstrates how the sequences of signs trigger the manipulation actions.

\( d_2 - d_3 \ldots \) to make two large effects on the block’s symbols: breaking the structure of the block by reordering its symbols and altering the individual symbols by modifying or mixing some of their bits. To perform these effects, the Manipulate operation uses the signs of the directives to execute four different actions on the block. Fig. 12 shows these four actions: Flip, LR Crossover, RL Crossover, and Scatter. Flip action negates the bits of the symbol. LR Crossover action causes the current symbol \( b_i \) to exchange the left half of its bits with the right half bits of the next symbol \( b_{i+1} \). RL Crossover action causes the current symbol \( b_i \) to exchange the right half of its bits with the left half bits of the next symbol \( b_{i+1} \). The Scatter action repositions the symbol \( b_i \) in the place specified by the directive \( d_i \).
are triggered. In particular, an action \( X \) is triggered based on a specific pattern of the current sign and the lookahead sign. Referring to Fig. 13, when the current sign is “+” and lookahead sign is also “+”, the Flip action is triggered and flips all the bits of the current input symbol \( b_i \). When the current sign is “-” and the lookahead symbol is “-”, the LR crossover action is triggered causing the right half bits of the current symbol \( b_i \) to exchange with the right half bits of the next symbol \( b_{i+1} \). When the current sign is “-” and the lookahead sign is “+”, the RL crossover action is triggered causing the right half bits of the current symbol \( b_i \) to exchange with the left half bits of the next symbol \( b_{i+1} \). Finally, when the current sign is “-” and the lookahead sign is “-”, the Scatter action is triggered causing the current symbol \( b_i \) to move to the index specified by \( d_i \).

It is clear that the former three actions (Flip and LR/RL Crossover) alter the individual symbols. While the latter action (Scatter) changes the structural relation between the symbols of the input block.

Second, the mask process introduces further masking to the block’s symbols by executing the directive-based masking operation. This operation does the masking by embedding the effects of the plain directives. In particular, the plain directives \( d_i \)’s (without the sign) are XORed with the corresponding block symbols to yield a masked block \( c_1c_2...c_n \). That is \( c_i = b_i \oplus d_i \) for \( i = 1, 2, ..., n \).

We illustrate the mask process using an example. Suppose for the sake of simplicity the following 4-byte block “77, 61, 6C, 6C”. Suppose further that the sequence of directives is “+30–7–18+3”. Fig. 14 shows the steps of masking this block. The leftmost column represents the index of the current input symbol—where “0” represents the index of the leftmost symbol in the input block. The second column shows the sequence of signs, where the currently considered sign pattern is shaded, and shows also the action performed (LR, S, etc.) based on the shaded sign pattern. The third column shows the input string (in Hex) and the input symbols which the corresponding action operates on. The rightmost column shows the sequence of directives. The manipulation process starts with the input symbol at index 0 (“77”) and the first sign pattern “+ +”. According to the logic in Fig. 13, this pattern triggers the LR Crossover action. The LR action therefore exchanges the left half bits of the current input symbol “77” with the right half bits of the next input symbol “61”, yielding the new block “17, 67, 6C, 6C”. Now, the second input symbol (at index 1) is “67” and the second sign pattern is “– +”. This sign pattern triggers the Scatter action, which moves the second input symbol “67” to the position specified by the plain directive of the second directive “– +”. That is, Scatter action moves “67” to the position \( 7 \% 4 = 3 \). (We take the module \% because the length of the input block is only four symbols.) Continuing likewise, the Manipulate operation produces the manipulated block “17, 6C, 66, 38”. The manipulated block is further masked by XORing the symbols with the plain part of the directives sequence. (Note the plain directives 30, 7, 18, 3 are transformed to Hex: 1E, 07, 12, 03.) The final output of the masking operation is “09, 6B, 74, 3B”.

The effect of the mask process is reversible provided that we have the directives sequence. To recover the original block, we define the inverse mask process. This process performs the same operations as the mask process, but in a reverse order. That is, the inverse mask process applies first the directive-based masking operation and then the Manipulate operation. The directive-based masking operation applies the XOR operation to the block and the plain directives \( d_i \)’s. The manipulation operation starts from the rightmost of the sign sequence and moves backwards (instead of starting from the leftmost). For instance, if the signs sequence is “+ + + + +” (in Hex), the inverse operation starts from the rightmost pattern “+ +” and the reverse operation starts from the rightmost pattern “+ +”, “+ +”, “+ +”, “+ +”, and “+ +”. The Flip, LR Crossover, and RL Crossover actions do not change. The Scatter action functionality is changed. Instead of moving the symbol \( b_i \) to the position \( d_i \% n \), the action moves the symbol at the position \( d_i \% n \) to the current index \( i \).

Fig. 15 shows an example of recovering the original block “77, 61, 6C, 6C” from the masked block “09, 6B, 74, 3B”. The sequence of directives is “+30–7–18+3” (“+1E–07–12+03” in Hex.) As the figure shows, the masking process applies first the directive-based masking operation to the input block “09, 6B, 74, 3B”, yielding “17, 6C, 66, 38”. The manipulation operation is then applied starting from the last sign pattern “+ +” and from the end of the input block. The pattern “+ +” triggers the Flip action, which flips all of the bits of the last symbol “38”, yielding the new block “17, 6C, 66, 37”. The current symbol now is “66” (at index 2) and the sign pattern is “- +”. This pattern triggers the RL crossover action, which causes the right half bits of the current input symbol “66” to be swapped with the left half bits of the following symbol “37”, yielding the new block “17, 6C, 66, 76”. The current symbol now is “66” (at index 1). The sign pattern is “- +”, which triggers the Scatter action. The symbol at the index 7 \% 4 = 3, which is “67”, is moved to the current index (position 1), yielding “17, 67, 6C, 6C”. Finally, the sign pattern “+ +” triggers the LR crossover action, which causes the symbol at the current index 0 (“17”) to exchange the left half of its bits with the right half bits of the next symbol at index 1 (“67”), yielding “77, 61, 6C, 6C”—the original block.
VII. THE CIPHER TECHNIQUE

This section presents the technical details of the proposed block cipher. Subsection VII-A presents how to use the operations defined in the previous sections to encrypt blocks of plaintext. Subsection VII-B presents how to decrypt the resulting ciphertext.

A. The Encryption Process

Let $B_i$ be plaintext block of size $n$ and Key be a key of size $m$, where $m$ is not necessarily equal to $n$. We impose no constraints on the size of the block. We also impose no specific constraints on the size of the key except those required for the key security. Therefore, a key size of 16 symbols or larger is highly recommended.

Initially, the encryption process prepares the D-Box and its inverse $D^{-1}$ as described in section II. This step is necessary for the functionality of the encryption operations and the key expansion.

After the D-Box is created, the encryption process executes as Fig. 16 shows. The process encrypts the block $B_i$ using the Key in $t$ rounds. It first expands the Key to size of $t \times n$ symbols, where $n$ is the size of the plaintext block $B_i$, and $t$ is the number of rounds. Each round applies the diffuse and substitute operations to the input block $B_i$ as described in sections II and IV. The outcome is passed to the mask operation. The mask operation receives also as an input a sequence of $n$ directives obtained from the directive generator. In order for the directive generator to produce these directives, it receives two inputs: the previous plaintext block $B_{i-1}$ and sub-key of size $n$ symbols. The sub-key symbols are obtained from the expanded key (EK[x: y]). The directive generator maps the symbols of the previous block $B_{i-1}$ to the mesh using the sub-key as described in Section V.

The encryption of the first block is handled slightly differently. That is because the first block $B_1$ has no predecessor block $B_{i-1}$. In this case, we use the $n$ symbols of the Key instead of the block $B_{i-1}$. Therefore, the same $n$ symbols of the Key are used as an input for both the Mapping and the Dimension selection operations.

B. The Decryption Process

The decryption process takes ciphertext and a key as an input and uses the key to produce the corresponding plaintext as an output. In order to accomplish this, the decryption process uses the inverse of the operations that are used during the encryption. The order in which the operations are applied is also reversed. Therefore, the decryption operations are executed in the following order: Inverse Mask, Inverse Substitute, and Inverse Diffuse. Fig. 17 shows the detailed steps of the decryption process. As the figure shows, the first operation to be applied to the input is the inverse mask operation instead of diffusion operation. The inverse substitute uses the $D^{-1}$ to reverse the effect of the substitution operation. Finally, the inverse diffuse operation is applied to reverse the effect of the diffusion operation.

In addition as Fig. 17 shows, the expanded key is used backwards. That is, the decryption process starts from the end of the expanded key (with $t \times n$ symbols) instead of starting from the beginning. Therefore, the decryption process uses the first $n$ key symbols from the right then the second $n$ symbols, and so on until the last left $n$ symbols. The sequences of directives are also used backwards. As Fig. 17 shows, the last


Fig. 16. the encryption process.

Fig. 17. the decryption process.

directive sequence in the encryption process “\(-z_1 + z_2 \cdots + z_n\)” is used first.

VIII. RELATED WORK

The most related encryption technique to ours is the advanced encryption standard (AES) [3]. The AES encrypts a block of plaintext in many rounds. The number of rounds depends on the size of the key. In each round, AES applies different operations: key round, substitution using S-Box, row shifting, column mixing, and so on. The AES technique is NIST’s standard [24]. Many researchers, however, reported major weaknesses. Specifically, the AES technique suffers from the weakness in the S-Box, making it more susceptible to computational attacks [5][19]. Several proposals have been suggested to improve the S-Box [6][20][21]. These proposals claimed to improve the effectiveness of the S-Box. The effectiveness of the S-Box is further enhanced in [22]. As claimed in [22], the new enhancement increases the algebraic complexity of the S-Box and therefore it becomes more immune against differential and algebraic attacks. These extensions, however, have their inherent drawbacks as pointed out in [5].

Despite the importance of these improvements and the work around methods, we believe that strengthening the substitution part of the encryption algorithms (Mainly AES) cannot be properly done by merely adding more mathematical transformations. We think the strength of the substitution must be based on the key as proposed by the technique herein. In other words, instead of having static substitution table (S-Box), it is more effective to have a more dynamic substitution operation whose state must depend on the key and change according to the changes of the this key (D-Box).

Data encryption standard (DES) and its successive improvements such as Triple DES [9][10] are symmetric block ciphers that follow Feistel cipher structure [30]. Their encryption model depends on applying a set of substitutions and manipulation operations augmented with key evolution. Although this algorithm is used to be a standard, its security challenged [23][25]. Even with fundamental improvement such as using two keys, the algorithm still suffers and its security is questioned in [23].

MARS, Blowfish, and Serpent [14][11][13] are symmetric block ciphers. Their encryption model depends like [9] on a set of substitutions and manipulation operations. Although their authors purport that these methods provide high levels of security, they failed to pass important randomness tests [27].

LEX encryption technique [16] is a stream cipher that is inspired by the one-pad encryption method (called also Vernam cipher). Although LEX claimed to have strong security properties, it uses the same round key repeatedly. This repeated use of the key makes it vulnerable to key-recovery attacks [28]. Our technique never uses the same key; each round uses a different version of the key and thus each block is encrypted using different keys.

Camellia encryption method [17] is a symmetric encryption technique, supporting 128-bit block size and 128, 192, 256-bit key. Efficiency on both software and hardware platforms is a remarkable characteristic of Camellia in addition to its high level of security. The main important difference between our technique and Camellia is that ours has more effective diffusion operation along with a dynamic substitution box.

To conclude this section, it is worth mentioning that
our proposed encryption method possesses several important characteristics that make it unique. First, in contrast to all encryption methods, our technique implicitly uses the key in every encryption operation. Second, our technique uses the plaintext to introduce further confusion to the encryption. In particular, it embeds the effect of the previous plaintext block in the encryption of the next block. As such, changes in the previous block impact not only the encryption of the previous block itself but the encryption of the next block as well; a feature that—to the best of our knowledge—is unique to our cipher. Third, our technique triggers the manipulation actions (these actions belong to the masking process) based on the signs of the directives. Since the signs of the directives depend on both the key and the plaintext blocks, the sequence of the triggering highly relies on the plaintext blocks and keys and greatly sensitive to their changes. This makes predicting the triggering order is infeasible. Finally, the functionality of our substitution operation changes with the changes of the key. This adds additional confusion layer, making the substitution step much more effective than the static substitution used by other encryption techniques.

IX. Performance Analysis

We present our performance analysis in this section. We first present an example that demonstrates some of our technique’s features and then analytically discuss its security properties in Subsection IX-B. We present the empirical evaluation in Subsection IX-C.

A. Encryption Example

We start our analysis by presenting examples of the technique’s output (ciphertext). The examples are meant to be simple but indicative. For the sake of simplicity, we assume that the plaintext blocks and the keys are of length 16 symbols. Fig. 18 shows the ciphertexts for the corresponding plaintexts, keys, and previous blocks. Referring to the figure, one can see that the output changes drastically when the input slightly changes. Consider for instance the first five rows, which are encrypted using the same key. Although these plaintexts differ in a single bit, their respective ciphertexts are greatly different. Changing a single bit in the key causes the ciphertexts for the same plaintexts to be really different (e.g. compare between the ciphertexts in rows 6 and 7). Finally, changing the previous block highly impacts the resulting ciphertexts. For instance, a quick look at rows 1 and 9 shows that changing a single bit in the previous block causes large changes to the ciphertexts of the same plaintext block.

This property of the proposed technique is very important. From one hand, a tiny change to any of the input (plaintext, key) results in extremely large changes to the respective ciphertexts. From the other hand, a tiny change to the previous plaintext block also largely impacts the ciphertext of the following plaintext block. From the security prospective, the proposed technique causes the relationship between plaintext and ciphertext to be so complicated and untraceable.

B. Analytical Performance Evaluation

The proposed technique has high confusion. The key is never explicitly used in the encryption; it is implicitly used via the directives. The key “trace” in the ciphertext is therefore so small to help predicting the used key. As such, the relationship between the key and the ciphertext is untraceable.

The proposed technique is highly sensitive to the changes of the input (see Fig. 18). This sensitivity provides an additional strong security guard. It makes the relationship between a key, ciphertext, and plaintext so complicated in a sense that if any of them changes, the respective ciphertext greatly changes. We attribute this high sensitivity to the changes of the input (plaintext or a key) to all the encryption operations (especially the diffuse and key expansion operations).

The state of the substitution box (D-Box) highly depends on the encryption key. Each different key results in a largely different new state and consequently results in different substitution outcomes. This means that changes of the key cause the same plaintext block to be substituted differently. This is in contrast to the other encryption algorithms (especially AES), where the substitution of a block is independent of the key. That is, the outcome of substituting a block remains the same regardless of the used key.

The key expansion operation adopts a highly complicated computational model. From one hand, the substitution sub-operation relates the process of substituting the current symbol to the outcome of substituting the proceeding symbols. This means that the outcome of the substitution for the current symbol $k_i$ is impacted by all the previous symbols $k_j$ ($j=1, 2, ..., i-1$). On the other hand, the key expansion manipulation sub-operation is highly complicated process. It partially depends on the order of the key’s symbols. For each new key, we have a new state (symbol order). In addition, the selection of the key’s manipulation operations depends on a random process. In other words, although the order of the symbols may bias the selection toward the operation with the higher ratio, the selection of the operation to be applied is nevertheless random. Even more, the random process is always seeded with latest version of the key. These properties assure that the key manipulation operations have a greatly complicated functional behavior in a sense that the number of states is tremendously large.

The mask process has perhaps the highest impact on its input block. It makes deep changes to both individual symbols and to the structure of the block, largely diverging the resulting block from the input block. The functionality of this operation fully depends on directive sequences. The manipulation operation, which modifies the individual symbols and the structure of the block, depends on the pattern of the signs of the directives. Since, this pattern depends on both the key and the previous block, it changes either the key or the previous block certainly results in a different pattern (regardless of the magnitude of the change) and consequently in a different functional behavior. Further the directive-based masking operation, which embeds the effect of the plain directive (value without the sign), depends also on the key and the previous block and changes according to their changes. As such, a change to the key or the previous block creates different modifications to the output of the masking operation.
C. Empirical Evaluation

We tested the performance of our encryption technique according to the testing rules specified by the national institute for standards and technology—NIST [27]. We specifically prepared the testing data as specified in [26].

1) Randomness Statistical Tests: We used the following tests to evaluate the randomness properties of our technique [27].

- **Runs test**: determines whether the number of runs of ones and zeros of various lengths is as expected for a random sequence.

- **Frequency Test (Monobit)**: determines whether the number of ones and zeros in a sequence are approximately the same as would be expected for a truly random sequence.

- **Discrete Fourier Transform Test (Spectral)**: detects periodic features (i.e. repetitive patterns that are near each other) in the tested sequence that would indicate a deviation from the assumption of randomness.

2) Randomness Hypotheses: We have two hypotheses to test:

- **$H_0$ (Null)**: the output of the encryption technique is random.

- **$H_1$ (Alternative)**: the output of the encryption technique is not random.

Accepting $H_0$ or $H_1$ depends on a computed value called p-value and a specified value called the significance level $\alpha$. The p-value is computed by the applied statistical test based on an input sequence. The significance level $\alpha$ is specified by the tester (e.g. 0.00001, 0.001, 0.01, 0.05 are typical values for $\alpha$). In particular if p-value $\geq \alpha$, $H_0$ is accepted ($H_1$ is rejected); otherwise $H_0$ is rejected ($H_1$ is accepted).

3) Test Data: The testing data were prepared according to [26]. Without losing the generality, we confine the D-Box to be 16 × 16. This allows for representing each symbol by 8 bits. We used the following sets of data to test our encryption technique.

1) **Key Avalanche Test**: The objective of this data set is to examine the sensitivity of our algorithm to changes in the key.

2) **Plaintext Avalanche Test**: The objective of this data set is to examine the sensitivity of our algorithm to changes in the plaintext.

3) **Plaintext/Ciphertext Correlation**: The objective of this data set is to study the correlation between plaintext–ciphertext pairs.

Fig. 18. The proposed technique output examples.
During the encryption, we set the number of rounds \( t \) to 8 rounds for each block because this number gives high performance. (Please see appendix A for more detailed discussion on the number of rounds \( t \).)

Tables II, III, and IV show the results of the applied randomness test to the above data sets. The tables show the applied tests, the number of sequences that passed the respective test, the number of failed sequences, and the rate of success. For each test, the significance level was fixed at 0.05, which implies that, ideally, no more than five out of hundred binary sequences may fail the corresponding test. However, in all likelihood, any given data set will deviate from this ideal case. A more realistic interpretation is to use a confidence interval (CI) for the proportion of binary sequences that may fail the corresponding test. The rightmost column shows the highest number of sequences that are expected to fail at the 0.05. The rightmost column shows the maximum number of binary sequences that are expected to fail the corresponding test. For instance, a maximum of 36.76 (actual 38, expected 36). Also, in Table IV, the number of the sequences that failed Spectral test is 35, which is very close to the maximum number of the sequences that are expected to fail.

### X. Conclusions and Future Work

We proposed a full-fledged encryption technique. This technique uses effective operations to manipulate blocks of plaintext and create deep changes to both the structure of the block and the individual symbols. By virtue of these operations, the technique ensures high diffusion, confusion, and avalanche effect. The performance numbers in subsection 9.3 clearly indicate the high avalanche effect. The technique has passed three NIST–recommended randomness tests for evaluating the effectiveness of encryption technique. In fact, the least percentage of the sequences that passed these tests was 91.7%.

We have two main objectives for future work. First, we want to replace the built-in random generator, which is used in the key expansion operation, with a more effective random generator. Second, we plan also to apply more randomness tests on a larger set of plaintexts and keys.

### References


A. Key-Based Numbers

We describe in this section how we generate the integers $I_i$ for reordering the content of D-Box. The process involves two steps.

1) **STEP I:** In this step, the encryption key is processed using the key handling procedure proposed by AES (advanced encryption standard). The AES key handling algorithm takes as input a 4-word (16-byte) key and produces a linear array of 44 words (176 bytes). The key is copied into the first four words of the expanded key. The remainder of the expanded key is filled in four words at a time. Each added word $w[i]$ depends on the immediately preceding word, $w[i-1]$, and the word four positions back, $w[i-4]$. In three out of four cases, a simple XOR is used. For a word whose position in the w array is a multiple of 4, a more complex function is used. Fig. 19 illustrates the generation of the first eight words of the expanded key, using the symbol $g$ to represent the complex function.

The function $g$ consists of the following sub-functions:

1) **RotWord** performs a one-byte circular left shift on a word. This means that an input word $[b_0, b_1, b_2, b_3]$ is transformed into $[b_1, b_2, b_3, b_0]$.

2) **SubWord** performs a byte substitution on each byte of its input word, using the static substitution box (or S-box)—See Fig. 20.

The result of steps 1 and 2 is XORed with a round constant, $Rcon[j]$. The round constant is a word in which the three rightmost bytes are always 0. Thus the effect of an XOR of a word with $Rcon$ is to only perform an XOR on the leftmost byte of the word. The round constant is different for each round and is defined as:

$$Rcon[j] = (RC[j], 0, 0, 0),$$


The multiplication is defined over the field $GF(2^8)$. The values of $RC[j]$ in hexadecimal are defined in Table V.

2) **STEP II:** In this step, the last 32 bytes (out of 176) of the sequence generated by Step I are used as a seed for the key-based number generator, which is described in [1]. Fig. 21 shows the algorithmic steps of the generator.

The key-based numbers are generated using the steps (2)–(5). As the figure shows, the symbols of the seed are summed


<table>
<thead>
<tr>
<th>j</th>
<th>RC[j]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>7</td>
<td>7</td>
</tr>
<tr>
<td>8</td>
<td>8</td>
</tr>
<tr>
<td>9</td>
<td>9</td>
</tr>
<tr>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>

**TABLE V. THE VALUES OF RC[j]**

by multiplying the integer value of each seed’s symbol $k_i$ by its position in the seed (step 2). The sum is then circularly left shifted $n$ positions to yield $S_h$ ($n$ is the value of the first two symbols in the seed) in step 3 and $S_h$ is XORed with the Sum in step 4 to yield $L_s$.

Assuming the number of symbols in the D-Box is $N$, the number $L_s$ is therefore adjusted by taking the module $N$. The seed is updated in step (5) by concatenating the seed with the current sum. The seed hence grows after each iteration. If, at any iteration, step (2) results in overflow in the sum, the procedure reduces the seed to 32 symbols by using the middle 32 unicode symbols as a new value for the seed. Steps (2) through (5) repeat until the condition no longer holds. (The condition determines the desired number of values to be generated.)

It is worth mentioning that the numbers created by the generator in Fig. 21 are random. The proof of the randomness properties of the generator in Fig. 21 is beyond the scope of this paper and can be found elsewhere [1].

**B. Number of Rounds ($t$)**

The number of the encryption rounds $t$, applied to each plaintext block, is very important and has a really large impact on the randomness properties of the output (ciphertext). More rounds (large values of $t$) result in higher diffusion and confusion (random output). More rounds, however, increase the time for encrypting a block. Thus, we look for a value for $t$ that achieves two objectives: (1) high randomness in the output and (2) short execution time.

To find the best number of rounds, we conducted many experiments, where we gradually increased the number of rounds from 1 to 10. We used in our experiments the same plaintexts in Section IX. For each value of $t$, we applied our encryption technique to 200 sequences each is of size 32,768 bits. We then subjected the resulting ciphertexts to three randomness tests (Runs, Monobit, and Spectral tests).

Table VI shows the results of the experiments. The results are presented in terms number of rounds $t$, the number of the sequences that passed the corresponding randomness test, and the rate of success. As the numbers show, there is a significant improvement in the success rate as $t$ increases from 1 to 8. When $t$ is greater than 8, the improvement in the success rate becomes slightly small. For instance, increasing the number of rounds from 8 to 9 slightly improves the rate of success (especially for Spectral), but this slight improvement causes really large increase in the time (see Fig. 22).

**Fig. 19.** The AES key handling procedure.

**Fig. 20.** The AES SBox.

**Fig. 21.** The algorithmic steps for generating key-based numbers.

![Fig. 20. The AES SBox.](image-url)
TABLE VI. **Changes in the Randomness Rate as the Number Rounds Increases**

<table>
<thead>
<tr>
<th>No. of Sequences</th>
<th>Rounds (t)</th>
<th>Test</th>
<th>Successes</th>
<th>Success Rate (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>1</td>
<td>Runs Test</td>
<td>100</td>
<td>50%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>25</td>
<td>12.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>0</td>
<td>0%</td>
</tr>
<tr>
<td>200</td>
<td>2</td>
<td>Runs Test</td>
<td>119</td>
<td>59.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>97</td>
<td>48.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>3</td>
<td>1.5%</td>
</tr>
<tr>
<td>200</td>
<td>3</td>
<td>Runs Test</td>
<td>122</td>
<td>61%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>96</td>
<td>48%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>3</td>
<td>1.5%</td>
</tr>
<tr>
<td>200</td>
<td>4</td>
<td>Runs Test</td>
<td>156</td>
<td>78%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>133</td>
<td>66.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>3</td>
<td>1.5%</td>
</tr>
<tr>
<td>200</td>
<td>5</td>
<td>Runs Test</td>
<td>183</td>
<td>91.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>167</td>
<td>83.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>58</td>
<td>29%</td>
</tr>
<tr>
<td>200</td>
<td>6</td>
<td>Runs Test</td>
<td>188</td>
<td>94%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>171</td>
<td>85.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>103</td>
<td>51.5%</td>
</tr>
<tr>
<td>200</td>
<td>7</td>
<td>Runs Test</td>
<td>192</td>
<td>96%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>182</td>
<td>91%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>147</td>
<td>73.5%</td>
</tr>
<tr>
<td>200</td>
<td>8</td>
<td>Runs Test</td>
<td>199</td>
<td>99.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>195</td>
<td>97.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>186</td>
<td>93%</td>
</tr>
<tr>
<td>200</td>
<td>9</td>
<td>Runs Test</td>
<td>200</td>
<td>100%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>197</td>
<td>98.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>188</td>
<td>94%</td>
</tr>
<tr>
<td>200</td>
<td>10</td>
<td>Runs Test</td>
<td>200</td>
<td>100%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Monobit</td>
<td>197</td>
<td>98.5%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Spectral</td>
<td>188</td>
<td>94%</td>
</tr>
</tbody>
</table>

Fig. 22. The time increase as a function of the number of rounds.