Post Treatment of Guided Wave by using Wavelet Transform in the Presence of a Defect on Surface

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Abstract—This article presents a Lamb wave processing by using two methods: Fast Fourier Transform (FFT2D) and Continuous Wavelet Transform (CWT) using Morlet wavelet. This treatment is done for a structure of two aluminum-copper plates, which are in contact edge to edge of a perpendicular junction with a thickness “e” in the presence of a rectangular and symmetrical defect located on the surface of the junction with a depth “d”. The aim under this study is to calculate the transmission and reflection energy coefficients by the two methods. The results of simulation obtained by Comsol software of an incident wave S₀ at F = 800 kHz indicate us a good coherence between the two methods (FFT2D and CWT).

Keywords—Lamb wave; defect; reflection; transmission; CWT; FFT2D

I. INTRODUCTION

Lamb [1] presents dispersion’s equation of Lamb waves that propagate in an elastic plate. This discovery would lead to many applications in different areas such as non-destructive testing. Recently, Viktorov [2] will devote a large part of his work to these waves called Lamb waves. Among the advantages of these waves, we find their propagation over a long distance that can attain a few hundred meters depending on the configuration of the structure and the frequency of the transducers used.

The relationship between the time and the displacements is obtained using the resolution of wave Lamb propagation equations.

These displacements are treated by FFT in order to extract dispersion’s curves and to convert incident wave into transmitted and reflected waves. Recently, we remark a significant use of wavelet transformation in domain of non-destructive control.

Wavelet analysis was introduced in the early 1980, it gives a representation of the signals allowing the simultaneous enhancement of the temporal and frequency information (time-frequency localization). Thus the need for wavelets, a family of functions deduced from the same function (called mother wavelets) by translation and dilation operation, was felt by noting that the Fourier transform which dominated from the beginning of 19th century, lost during the projection the control of the temporal variable during the projection and is still unable to describe locally (in time or space) the frequency behavior of the signals.


Kaihong Zheng et al [7] proposed a non-destructive testing and evaluation (NDE) method based on Lamb waves in order to detect damage in stiffened composite panels. Jinrui Zhang et al [8] are employed the CWT to analyze the Lamb wave dispersion of the detected signal. Bo Feng et al [9] are presented a method that is able to detect and assess delamination's length in anisotropic CFRP plates using chirp-excited Lamb wave and wavelet analysis. Faeetz A. Masurkara and Nitesh P. Yelve [10] are carried out on an aluminum plate with and without damage using Lamb wave in order to locate single as well as multiple damage based on wavelet transform algorithm. Michele Carboni et al [11] are studied the propagation of Lamb wave for quasi-isotropic CFRP laminate with the aim to set-up a “single propagation mode” approach. Guoji Zhao et al [12] are used ultrasonic guided wave in order to detect the delamination of composite double cantilever beams (DCBs). The study of Zhongqing Su et al [13, 14] based on a Lamb wave propagation-based delamination identification scheme for CF/EP composite structures [13] to detect delamination in the structures. Then they are focused on their study to provide a comprehensive on the Lamb wave-based damage identification approaches for composites structures [14].

Among the treatment that used FFT we find, Taoufiq Belhoussine Drissi et al [15] that studied the reflection and the transmission of guided wave at the right junction of two different elastic plates with the presence of a defect, and Mouna Seddiki, Hakim Djelouah [16] which their study focus on the identification of propagative Lamb mode in a plate with the presence of a defect.
For the treatment used by WT we find, Beata Zima and Magdalena Rucka [17] that presented an experimental study of guided wave propagation on a steel plate with an internal defect by using continuous wavelet processing to obtain accurate reconstruction of reflected waves, and a study proposed by D. Waltisberg, R. Raisūtis [18] based on the separation of the first symmetric mode \( S_0 \) and the first asymmetric mode \( A_0 \) and the reliable estimation of their group velocities by using tree methods among them the wavelet transform. LeiYang, I. CharlesUme [19] are used CWT for a thin steel plate in order to calculate the transmission coefficients of laser-generated Lamb waves. Taoufiq Belhoussine Drissi et al [20] are used the wavelet transform for a speech signal in order to determine the choice of the appropriate wavelet analyzer with the method of extraction of MFCC coefficients for an assistance in the diagnosis of Parkinson’s disease. Tsun-Yen Wu [21] et al are used the CWT to help identify wave packets of the \( S_0 \) and \( A_0 \) Lamb wave modes in order to detect defects in thin structures. Lei Yang, I et al [22] are used the LEU technique to inspect the notch depths in thin steel plates and by the CWT they computed the transmission coefficient of Laser generated Lamb wave.

Another research used both the FFT and CWT, among them M. Sifuzzaman [23] that compared analytically the advantages of the wavelet transform according to the Fourier transform and also Mhammed El Allami and Hassan Rhimini [24] that used the wavelet transformation to determine the energies of the different Lamb modes propagating in a steel plate with an internal, rectangular and symmetrical defect with respect to the axis of propagation.

In the present work, we come up with a treatment by the continuous wavelet and Fourier transform (CWT and FFT2D) for two isotropic and thin plates aluminum-copper which are connected to each other by a perpendicular junction with the presence of a rectangular and symmetrical defect on the surface of the junction. The objective of this treatment is to calculate the reflection and transmission energy coefficients, then compare the results obtained by the two methods (FFT2D and CWT).

II. PRESENTATION OF THE STUDIED STRUCTURE

For this treatment, we use the structure below:

The structure contains two isotropic and thin plates aluminum-copper which are in contact edge to edge with thickness \( e = 2 \text{mm} \) in the presence of a rectangular defect with depth \( d \) and located symmetrically on the median plan.

Aluminum is indicated by index 1 and characterized by the density \( \rho_1 \), a longitudinal \( c_{11} \) and transversal velocity \( c_{11} \). Copper is indicated by index 2 and characterized by the density \( \rho_2 \), a longitudinal \( c_{22} \) and transversal velocity \( c_{22} \).

The table below presents the characteristics of aluminum and copper plates:

<table>
<thead>
<tr>
<th>Characteristics</th>
<th>Aluminum</th>
<th>Copper</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density (kg/m(^3))</td>
<td>2799</td>
<td>8705</td>
</tr>
<tr>
<td>Transversal velocity (m/s)</td>
<td>3115</td>
<td>2360</td>
</tr>
<tr>
<td>Longitudinal velocity (m/s)</td>
<td>6320</td>
<td>4728</td>
</tr>
</tbody>
</table>
The distribution of the energy of the incident mode between the reflected and transmitted mode is done by calculating the magnitude of each mode.

The superposition of the theoretical dispersion curves on those obtained by FFT2D show us that at the frequency F = 800 kHz, we have just the symmetrical mode S₀ while the junction is symmetrical.

V. TREATMENT BY THE WAVELET TRANSFORM METHOD

The CWT has been developed to overcome some resolution defaults of the Fourier Transform. It is able to provide a simultaneous time-frequency representation of the signal. In 1982, Morlet [26] opened the way to the solution by building the wavelet transform.

The continuous wavelet transform uses two parameters: one called the scale of the wavelet “a”, it can give different version of wavelets by compressing, and dilating the same mother wavelet, it presents the inverse of the frequency. The other is the translation parameter “b” which translates the wavelet along the time axis of the signal. The continuous wavelet transform of a signal s(t) is defined by:

$$ W(a,b) = \int_{-\infty}^{\infty} \psi^{*} \left( \frac{t-b}{a} \right) s(t) dt $$

(1)
Where: Ψ(t) is the wavelet function, Ψ*(t) is Ψ(t) complex conjugate, W(a,b) are the continuous WT coefficients.

We apply the continuous wavelet transform by using the mother wavelet Morlet for displacements collected at points situated before the defect (x = 40mm) and after the defect (x = 110mm) in order to obtain the 3D plot of wavelet coefficients. See Fig. 8 and Fig. 9.

In general, the maximum wavelet coefficient depends on the shape of the wavelet; when the section of the signal has the same shape as the wavelet, we obtain the maximum value of the wavelet coefficients.

In our case, we confirm that a = 10 corresponding to the maximum value of coefficients wavelet as shown in Fig. 10 and Fig. 11, then the row of the coefficient matrix for this scale was plotted as function of time. See Fig. 12 and Fig. 13.

After the determination of the magnitudes of incident, reflected and transmitted mode for each method (Fig. 5, Fig. 7 for the FFT2D and Fig. 12, Fig. 13 for CWT), now we can deduce the reflection and transmission energy coefficients by applying the following equations [15, 24].

\[
R(S_i) = \frac{(A^R(S_i)*\zeta^i(S_i))^2}{(A^i(S_i)*\zeta^R(S_i))^2}
\]

\[
T(S_i) = \frac{(A^t(S_i)*\zeta^i(S_i))^2}{(A^i(S_i)*\zeta^t(S_i))^2}
\]
Where: $A^1$, $A^2$ and $A^3$ are the magnitudes of the modes where the higher index present respectively incident, reflected and transmitted mode. The coefficients $\zeta$ are defined by the module of the normal displacement on the surface of the plate divided by the square root of Poynting vector [11].

$$\zeta = \frac{U_z}{\sqrt{\phi}}$$  \hspace{1cm} (4)

VI. RESULTS OF THE TWO PROCESSING

The transmission and reflection energy coefficients obtained by the two methods (FFT2D and CWT) in the case of the incident mode is the symmetrical mode $S_0$ at frequency $f=800$kHz in the presence of a defect, where the report of the depth of defect by the thickness of the plate is ($d/e = 1\%$, 2\%, 3\%, 4\% and 5\%) are presented in the following Fig. 14:

The continuous curve in blue indicate the reflection energy coefficient obtained by FFT2D and the curve with stars is the reflection energy coefficient obtained by CWT.

The continuous curve in red indicate the transmission energy coefficient obtained by FFT2D and the curve with stars is the reflection energy coefficient obtained by CWT.

The continuous curve in black indicate the energy conservation $R+T$ obtained by FFT2d and the curve with stars is the energy conservation obtained by CWT.

This figure indicates that the results of the two methods in presence of a defect with ($d/e = 1\%$, 2\%, 3\%, 4\% and 5\%) are identical with a neglected error, and an energy conservation $R+T \approx 1$. We can deduce that there is a good coherence between FFT2D and CWT and when the report $d/e$ increase the reflection energy coefficient increase and the transmission energy coefficient decrease.

![Fig. 14. Transmission and Reflection Energy Coefficients and Energy Conservation.](image)

VII. CONCLUSION

In this paper, we proposed a treatment of Lamb wave for a two aluminum-copper plates, which are in contact edge to edge by a perpendicular junction with an internal, rectangular and symmetrical defect. This processing is done by two methods: the Continuous Wavelet Transform (CWT) and the Fast Fourier Transform (FFT2D) in order to calculate the reflection and transmission energy coefficients. The obtained results showed us a good coherence between the two methods (FFT2D and CWT). By increasing the thickness of the defect, the reflection energy coefficient increased and the transmission energy coefficient decreased. As prospect, we can use other mother wavelet such us Coifman, Daubechies etc.

REFERENCES


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