Novel Properties for Total Strong - Weak Domination Over Bipolar Intuitionistic Fuzzy Graphs

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Abstract—Through this research study, we introduced and discussed total strong (weak) domination concept of bipolar intuitionistic fuzzy graphs and in define strong domination bipolar intuitionistic fuzzy graph also strong domination. Theorems, examples and some properties of these concept are discussed.

Keywords—Fuzzy sets; bipolar intuitionistic fuzzy sets; strong (weak) bipolar intuitionistic fuzzy sets; total strong (weak) bipolar intuitionistic number

I. INTRODUCTION

The theory of fuzzy sets was introduced by Zadeh [1]. On this notion the researchers emphasized their applications in different areas such as electrical engineering economics, Computer Science, social networks, system analysis and mathematics, many researchers using this concept to generalized and study some topics [2-8]. Atanassov [9] generalized the idea of fuzzy set and gave new Concept which intuitionistic fuzzy sets. Many researchers have benefited from this new Concept in developing many old Concepts in many fields of Science [10-13]. Zhang [14] initiated a bipolar fuzzy this new Concept in developing many old Concepts in developing intuitionistic fuzzy sets. Many researchers have used this notion to study many properties [15-18]. Ezhilmaran and Sankar [19 - 20] have introduced bipolar intuitionistic fuzzy graph and strong domination bipolar intuitionistic fuzzy graph also strong domination. Theorems, examples and some properties of these concepts will also be discussed.

II. PRELIMINARIES

Definition 2.1: [1] Let G be a set, a fuzzy set \( \delta \) on \( G \) just function: \( \delta : G \rightarrow [0,1] \).

Definition 2.2: [3] A fuzzy set \( \delta \) is said to be fuzzy relation on \( G \) if the map \( \gamma : G \times G \rightarrow [0,1] \) satisfy \( \gamma (a,d) \leq \min\{\delta (a), \delta (d)\} \) for all \( a, d \in G \). A fuzzy relation is symmetric if \( \gamma (a,d) = \gamma (d,a) \) for all \( a, d \in G \).

Definition 2.3: [14] If \( G \neq \emptyset \). A bipolar fuzzy set \( \lambda \) of \( G \) is object with form \( \varphi = \{(i, \lambda^+(i), \lambda^-(i)); i \in G\} \) such that \( \lambda^+: G \rightarrow [0,1] \) and \( \lambda^-: G \rightarrow [-1,0] \) are mappings.

Definition 2.4: [9] If \( G \) is an empty set. An intuitionistic fuzzy set \( S = \{(k; \mu(k), \lambda(k); k \in G)\} \) such that \( \mu : G \rightarrow [0,1] \) and \( \lambda : G \rightarrow [0,1] \) are mapping such that \( 0 \leq \mu (k) + \lambda (k) \leq 1 \).

Definition 2.5: [24] An ordered pair \( G^* = (V,E) \) is graph such that \( V \) the vertices set in \( G^* \) & \( E \) the edge set in \( G^* \).

Remark 2.6: [24] 1) If \( c \) and \( e \) are two vertices in \( G^* \) then its called adjacent of \( G^* \) when \( (c,e) \) is edge of \( G^* \).

2) An undirected graph which has at most one edge between any two different vertices no loops called simple graph.

Definition 2.7: [24] A sub graph of \( G^* \) is a graph \( S = (W,F) \) such that \( W \subseteq V \) and \( F \subseteq E \).

Definition 2.8: [24] \((G^*)^c\) is complementary graph of a simple graph with the same vertices of \( G^* \).

Remark 2.9: [24] Two vertices are adjacent in \( (G^*)^c \) iff they are not adjacent in \( G^* \).

III. MEAN RESULTS

Definition 3.1: [19] If \( G \neq \emptyset \). A bipolar intuitionistic fuzzy sets \( S = \{(e; \mu^+(e), \mu^-(e), \lambda^+(e), \lambda^-(e); e \in G\} \) such that \( \mu^+: G \rightarrow [0,1] \), \( \mu^-: G \rightarrow [-1,0] \), \( \lambda^+: G \rightarrow [0,1] \), \( \lambda^-: G \rightarrow [-1,0] \) are mapping, where \( 0 \leq \mu^+(e) + \lambda^+(e) \leq 1 \), \( -1 \leq \mu^-(e) + \lambda^-(e) \leq 0 \).

Using the degree of positive membership \( \mu^+(i) \) to represent the degree of satisfaction of \( "e" \) to the corresponding of property of a bipolar intuitionistic fuzzy sets \( S \) also the negative degree of membership \( \mu^-(e) \) for represent the satisfaction degree of \( "e" \) for any implicit counter property corresponding for a bipolar intuitionistic fuzzy sets. By the same cases, we use the degree of positive non membership \( \lambda^+(e) \) represent the satisfaction degree of \( "e" \) to the property corresponding for a bipolar intuitionistic fuzzy sets also, the degree of negative non membership \( \lambda^-(e) \) for represent the satisfaction degree "e" to some implicit counter property corresponding for a bipolar intuitionistic fuzzy sets.

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672 | P a g e
If $\mu^+(e) \neq 0, \mu^-(e) = 0$ and $\lambda^+(e) = 0, \lambda^-(e) = 0$ the situation that "$e$" regarded as have only a positive membership property in bipolar intuitionistic fuzzy sets. While if $\mu^+(e) = 0, \mu^-(e) \neq 0$ also $\lambda^+(e) = 0, \lambda^-(e) = 0$, then it's the situation that "$e$" regarded as have a negative member - ship property. While if $\mu^+(e) = 0, \mu^-(e) = 0$ also $\lambda^+(e) \neq 0, \lambda^-(e) = 0$, it's the situation that "$e$" regarded as have only a positive non member - ship property. If $\mu^+(e) = 0, \mu^-(e) = 0$ also $\lambda^+(e) = 0, \lambda^-(e) \neq 0$ when a member - ship and non member - ship function of a property overlaps with its counter properties over one portion of "$e$".

**Definition 3.2:** [19] If $G$ is an empty set. Then the mapping $\mathcal{J} = (\mu_1^+, \mu_2^-, \lambda_1^+, \lambda_2^-): G \times G \to \{0, 1\} \times [-1, 0] \times [0, 1] \times [-1, 0]$ is a bipolar intuitionistic fuzzy relation on $G$, where $\mu_1^+(i, j) \in [0, 1], \mu_2^-(i, j) \in [-1, 0], \lambda_1^+(i, j) \in [0, 1]$ and $\lambda_2^-(i, j) \in [-1, 0]$.

**Definition 3.3:** [19] Let $\mathcal{J}_1 = (\mu_1^+, \mu_2^-, \lambda_1^+, \lambda_2^-)$ be a bipolar intuitionistic fuzzy sets on $G$. $\mathcal{J}_1$ is a bipolar intuitionistic fuzzy relation for $\mathcal{J}_2$ if

1) $\mu_1^+(i, j) \leq \mu_2^-(i, j)$
2) $\lambda_1^+(i, j) \geq \lambda_2^-(i, j)$
3) $\forall e, f \in G$. $\mu^+(e, f) \leq \mu^-(e, f)$
4) $\lambda^+(e, f) \geq \lambda^-(e, f)$
5) $\lambda^+(e, f) \leq \lambda^-(e, f)$

**Remark 3.4:** A bipolar intuitionistic fuzzy relation for $\mathcal{J}_3$ on $G$ is said to be symmetric when $\mu_1^+(i, j) = \mu_2^-(i, j)$, $\mu_2^+(i, j) = \mu_2^+(i, j)$ and $\lambda_2^+(i, j) = \lambda_2^+(i, j)$.

**Definition 3.5:** [19] A bipolar intuitionistic fuzzy graph of $G^* = (V, E)$ that is a pair $G = (X, Y)$ such that $\mathcal{J}_1 = (\mu_1^+, \mu_2^-, \lambda_1^+, \lambda_2^-)$ is a bipolar intuitionistic fuzzy sets in $V$ and $\mathcal{J}_2 = (\mu_2^+, \mu_2^-, \lambda_2^+, \lambda_2^-)$ is a bipolar intuitionistic fuzzy set of $V \times V$ such that:

1) $\mu_1^+(e, f) \leq \min\{\mu_1^+(e, f), \mu_2^+(e, f)\}, \forall e, f \in V \times V$
2) $\mu_2^+(e, f) \geq \max\{\mu_2^-(e, f), \mu_2^-(e, f)\}, \forall e, f \in V \times V$
3) $\lambda_1^+(e, f) \geq \max\{\lambda_1^+(e, f), \lambda_1^+(e, f)\}, \forall e, f \in V \times V$
4) $\lambda_2^+(e, f) \leq \min\{\lambda_2^-(e, f), \lambda_2^-(e, f)\}, \forall e, f \in V \times V$
5) $\mu_2^+(e, f) = \mu_2^-(e, f) \leq 0, \forall e, f \in V \times V$
6) $\lambda_2^+(e, f) = \lambda_2^-(e, f) \leq 0, \forall e, f \in V \times V$

Through this article, $G^*$ and $G$ is representing a crisp to a graph and bipolar intuitionistic fuzzy graph respectively.

**Definition 3.6:** Let $F = (\mathcal{J}_1, \mathcal{J}_2)$ be a bipolar intuitionistic fuzzy graphs, where $\mathcal{J}_1 = (\mu_1^+, \mu_2^-, \lambda_1^+, \lambda_2^-)$ and $\mathcal{J}_2 = (\mu_2^+, \mu_2^-, \lambda_2^+, \lambda_2^-)$ are two bipolar intuitionistic fuzzy set on a non empty set $V$ and $\mathcal{J}_1 \subseteq V \times V$.

The positive degree of a vertex $\mu_1^+(i, j), \lambda_1^+(i, j) \in G$ is $D^+(\mu_1^+, \lambda_1^+) = \sum_{e \in \mathcal{E}} \mu_1^+(e, f) + \sum_{f \in \mathcal{E}} \lambda_1^+(e, f)$

Similarly, the negative degree of a vertex $\mu_1^-, \lambda_1^- \in G$ is $D^- = \sum_{e \in \mathcal{E}} \mu_1^-(e, f) + \sum_{f \in \mathcal{E}} \lambda_1^-(e, f)$

The degree of the vertex is $D(\mu, \lambda) = (D^+(\mu, \lambda), D^-(\mu, \lambda))$.

**Definition 3.7:** If $G = (\mathcal{J}_1, \mathcal{J}_2)$ is a bipolar intuitionistic fuzzy graphs. Then the bipolar intuitionistic fuzzy graph $G$ order given by $O(G) = (\Sigma_{e \in \mathcal{E}} \mu_1^+(e, f), \Sigma_{f \in \mathcal{E}} \mu_1^-(e, f), \Sigma_{e \in \mathcal{E}} \mu_2^+(e, f), \Sigma_{f \in \mathcal{E}} \mu_2^-(e, f), \Sigma_{e \in \mathcal{E}} \mu_1^-(e, f), \Sigma_{f \in \mathcal{E}} \mu_2^+(e, f))$.

The size of a bipolar intuitionistic fuzzy graph $G$ is $\mathcal{S}(G) = (\Sigma_{e \in \mathcal{E}} \mu_1^+(i, j), \Sigma_{f \in \mathcal{E}} \mu_1^-(i, j), \Sigma_{e \in \mathcal{E}} \mu_2^+(i, j), \Sigma_{f \in \mathcal{E}} \mu_2^-(i, j))$.

**Definition 3.8:** If $G = (\mathcal{J}_1, \mathcal{J}_2)$ is a bipolar intuitionistic fuzzy graph, for each node in node $G$ has the same closed degree of neighborhood, thus $G$ said to be totally bipolar intuitionistic fuzzy graphs. The closed degree of neighborhood of a node "$e$" defined as $Deg(e) = (Deg^+(e) + Deg^-)$, such that $Deg^+(e) = (Deg^+(e) + \mu_1^-(e, f) + Deg^-(e))$

$Deg^-(e) = (Deg^- + \mu_2^+(e, f) + Deg^+(e))$

**Definition 3.9:** A bipolar intuitionistic fuzzy graphs $G = (\mathcal{J}_1, \mathcal{J}_2)$ is called strong bipolar intuitionistic fuzzy graph, when $\mu_1^+(i, j) = \sum_{i, j} \mu_1^+(i, j), \mu_2^+(i, j) = \sum_{i, j} \mu_2^+(i, j)$ and $\mu_1^-(i, j) = \sum_{i, j} \mu_1^-(i, j)$ and $\mu_2^-(i, j) = \sum_{i, j} \mu_2^-(i, j)$.

**Definition 3.10:** If $G = (\mathcal{J}_1, \mathcal{J}_2)$ is a bipolar intuitionistic fuzzy graph, if $I$ and $J$ are two vertices. Then $I$ is totally strongly dominates $J$ (I totally weakly dominates J)

If

1) $\mu_1^+(e, f) = \mu_1^-(e, f)$
2) $\mu_2^+(e, f) = \mu_2^-(e, f)$
3) $\lambda_1^+(e, f) = \lambda_1^-(e, f)$
4) $\lambda_2^+(e, f) = \lambda_2^-(e, f)$

Every vertex in $G$ dominates $I$.

**Definition 3.11:** If $G$ is a bipolar intuitionistic fuzzy graph; $\tau_B$ is called total strong ( weak ) dominating a bipolar intuitionistic set of G if
1) $\mu(H, S) \geq \mu^\omega(H, S), \lambda(H, S) \geq \lambda^\omega(H, S) \forall H, S \in V(G)$

2) $D^-(H) \supseteq D^-(S) \forall H \in \tau_B, S \in V - \tau_B$

3) $\mu^+_{\lambda}(ef) = \min\{\mu_{\lambda_1}(e), \mu_{\lambda_1}(f)\}$

$\lambda_{\lambda_2}^+(ef) = \max\{\lambda_{\lambda_2}(e), \lambda_{\lambda_2}(f)\}$ and

$\lambda_{\lambda_2}^-(ef) = \max\{\lambda_{\lambda_2}(e), \lambda_{\lambda_2}(f)\}; \forall e, f \in E$

4) $\tau_B$ is the total dominating set of a bipolar intuitionistic fuzzy graph

$\text{Definition 3.12:} \tau_B$ of a fuzzy graph $G$ is called minimal total strong (weak) dominating bipolar intuitionistic set of $G$, if there doesn’t exist any total strong (weak) dominating bipolar intuitionistic set of $G$, whose cardinality is less than the cardinality $\tau_B$

$\text{Definition 3.13:}$ A total strong (weak) dominating bipolar intuitionistic set in $G$ is the fuzzy cardinality of minimum among all minimal total strong (weak) dominating bipolar intuitionistic set $G$.

$\text{Remark 3.14:}$ The total strong (weak) domination bipolar intuitionistic number is represented by $\pi_{\tau_B}(G)$.

$\text{Example 3.15:}$ If $G$ is a bipolar intuitionistic fuzzy graph given by the Fig. 1.

Total strong (weak) dominating bipolar intuitionistic set $\tau_B = \{x, y\}$

Total strong (weak) bipolar domination number $\pi_{\tau_B}(\mu_{\lambda_1}, \mu_{\lambda_1}, \lambda_{\lambda_1}, \lambda_{\lambda_1}) = (1.1, -0.7, 1, -0.9)$

$\text{Degree (} \mu_{\lambda_1}, \mu_{\lambda_1}, \lambda_{\lambda_1}, \lambda_{\lambda_1}) = (0.8, -0.4, 0.9, -0.6)$

$\text{Degree (} \mu_{\lambda_1}, \mu_{\lambda_1}, \lambda_{\lambda_1}, \lambda_{\lambda_1}) = (0.5, -0.3, 1, -0.4)$

$\text{Degree (} \mu_{\lambda_1}, \lambda_{\lambda_1}, \mu_{\lambda_1}, \lambda_{\lambda_1}) = (0.4, -0.5, 1, -0.7)$

$\text{Degree (} \mu_{\lambda_1}, \lambda_{\lambda_1}, \mu_{\lambda_1}, \lambda_{\lambda_1}) = (0.7, -0.6, 0.9, -0.9)$

$\text{Order of bipolar intuitionistic fuzzy graph } O(G) = (2.1, -1.7, 1.7, -1.5)$

$\text{Size of bipolar intuitionistic fuzzy graph } S(G) = (1.2, -0.9, 1.9, -1.3)$

$\text{Theorem 3.16:}$ If $G$ is bipolar intuitionistic fuzzy graph also if $\tau_B$ is minimal total strong (weak) dominating. Then for each $J \in \tau_B$, if one of following axioms hold

1) There is no vertex of $\tau_B$ strongly dominates $J$

2) $\exists J \in V - \tau_B$ is the only vertex in $\tau_B$ which strongly dominates $J$

3) $\tau_B$ is bipolar intuitionistic fuzzy graph with total dominating set.

$\text{Proof:}$ Suppose that $\tau_B$ is a minimal total strong (weak) dominating set. Then for every $J \in \tau_B, \tau_B - \{J\}$ is not a total strong (weak) dominating set, then there exist $I \in V - \tau_B$, such that not strongly dominated by any vertex belong to $\tau_B - \{J\}$. Since $\tau_B$ is total strong dominating set. Thus $J$ is only vertex which strongly dominates $J$ and hence axiom 2 hold.

Now, suppose that $\tau_B$ be total strong (weak) dominating set also for each $J \in \tau_B$ thus one of the following two axioms holds

If $\tau_B$ not minimal, then $\exists J \in \tau_B, \tau_B - \{J\}$ a total strong dominating set also hence $J$ is strongly dominated by at least one vertex in $\tau_B - \{J\}$ and its contradiction by 1.

If $\tau_B - \{J\}$ is a total strong (weak) dominating, then every vertex belong to $V - \tau_B$ is totally strongly (weak) dominated by at least one vertex belong to $\tau_B - \{J\}$. The second condition does not holds. This $\tau_B$ a minimal total strong (weak) dominating set.

$\text{Corollary 3.17:}$ All complete bipolar intuitionistic fuzzy graph also total strong (weak) domination in bipolar intuitionistic fuzzy graphs.

$\text{Proof:}$ $G$ be complete bipolar intuitionistic fuzzy graphs. Thus every edge is total strong (weak) dominating set also every vertices are join together. Thus and obvious, $G$ be total strong (weak) dominating set.

$\text{Example 3.18:}$ Given a bipolar intuitionistic fuzzy graphs $G$ given by Fig. 2 and 3.
\[ \tau_B - \{Z\}, \pi_{\tau_B} - \{G\} = (0.2, -0.1, 0.5, -0.6) \]
\[ \tau_B - \{W\}, \pi_{\tau_B} - \{G\} = (0.3, -0.1, 0.7, -0.9) \]

**Definition 3.19:** A bipolar intuitionistic fuzzy graphs \( G \) is said to be a semi-\( \gamma \)-strong bipolar intuitionistic fuzzy graph when
\[ \mu_{\tau_1}^+(e, f) = \min\{\mu_{\tau_1}^+(e), \mu_{\tau_2}^+(f)\} \]
and
\[ \mu_{\tau_2}^-(e, f) = \min\{\mu_{\tau_1}^-(e), \mu_{\tau_2}^-(f)\} \]
for every \( e \) and \( f \).

**Theorem 3.20:** Let \( G \) be a bipolar intuitionistic fuzzy graph on order \( O(G) \) then
\[ 1) \quad \beta_{\text{bsbf}}(G) \leq \beta_{\text{tsbf}}(G) \leq O(G) - \Delta_n(G) \leq O(G) - \Delta_e(G) \]
\[ 2) \quad \beta_{\text{bsbf}}(G) \leq \beta_{\text{twbf}}(G) \leq O(G) - \delta_n(G) \leq O(G) - \delta_e(G) \]

Where \( \beta_{\text{bsbf}}, \beta_{\text{tsbf}} \) and \( \beta_{\text{twbf}} \) represent to strong bipolar intuitionistic domination, total strong bipolar intuitionistic domination and total strong (weak) bipolar intuitionistic domination respectively.

**Proof:** Hence \( G \) every \( \beta_{\text{bsbf}} - \text{set} \) is a bipolar intuitionistic dominating set \( \beta_{\text{bsbf}}(G) \leq \beta_{\text{tsbf}}(G) \) and \( \beta_{\text{twbf}}(G) \leq \beta_{\text{twbf}}(G) \) if \( i, j \in V \) and \( D_n(i) = \Delta_n(G) \) and \( D_n(j) = \delta_n(G) \) then \( V - N(i) \) is a \( \beta_{\text{tsbf}} - \text{set} \) but not minimal and \( V - N(j) \) is \( \beta_{\text{twbf}} - \text{set} \) but not minimal.
hence $\mathcal{I}_{sbf}(G) \leq |V - N(i)|_{sbf}$ this means that $|V - N(i)|_{sbf} = |V| - |N(u)|$
\[ \Rightarrow O(G) - D_n(u) \]
\[ \Rightarrow O(G) - \Delta_n(G) \]
\[ \Rightarrow \mathcal{I}_{sbf}(G) \leq O(G) - \Delta_n(G) \] and $\mathcal{I}_{wbf}(G) \leq |V - N(i)|_{wbf}$
\[ \text{this means that } |V - N(j)|_{wbf} = |V| - |N(j)| \]
\[ \Rightarrow O(G) - D_n(j) \]
\[ \Rightarrow O(G) - \Delta_n(G) \]
\[ \Rightarrow \mathcal{I}_{wbf}(G) \leq O(G) - \Delta_n(G) \]

More over, $\Delta_e(G) \leq O(G)$ and $\delta_e(G) \leq \delta_n(G)$
\[ \Rightarrow \mathcal{I}_{sbf}(G) \leq \mathcal{I}_{sbf}(G) \leq O(G) - \Delta_n(G) \]
\[ \leq O(G) - \Delta_n(G) \]
\[ \Rightarrow \mathcal{I}_{wbf}(G) \leq \mathcal{I}_{wbf}(G) \leq O(G) - \delta_n(G) \leq O(G) - \delta_e(G) \]

**Corollary 3.21:** If $G$ is a bipolar intuitionistic fuzzy graph, then $\mathcal{I}_{sbf}(G) \leq \mathcal{I}_{wbf}(G)$.

**Proof:** If $x, y$ is a minimal total and strong weak dominating set respectively. If $D_n(i) = \Delta_n(G)$ and $D_n(j) = \delta_n(G)$ not that $V - N(j)$ is a total weak domination.

Example 4.1

\[ \mathcal{I}_{wbf}(G) \leq |V - N(i)|_{wbf} \]
\[ \mathcal{I}_{wbf}(G) \leq O(G) - \Delta_n(G) \] and $\mathcal{I}_{wbf}(G) \leq |V - N(i)|_{wbf}$
\[ \mathcal{I}_{wbf}(G) \leq O(G) - \delta_n(G) \]

Since $O(G) - \Delta_n(G) \leq O(G) - \delta_n(G)$ we get
\[ \mathcal{I}_{wbf}(G) \leq \mathcal{I}_{wbf}(G) \]

**Corollary 3.22:** For a bipolar intuitionistic fuzzy graph $G$

1) $O(G) - S(G) \leq \mathcal{I}_{wbf}(G) \leq O(G) - \delta_e(G)$.
2) $O(G) - S(G) \leq \mathcal{I}_{wbf}(G) \leq O(G) - \Delta_e(G)$.

**Proof:** Straight forward.

Note 3.23: Let $G$ is a bipolar intuitionistic fuzzy graphs such that every vertex having a same membership grade, then

1) $O(G) - S(G) \leq \mathcal{I}_{wbf}(G) \leq O(G) - \delta_e(G)$.
2) $O(G) - S(G) \leq \mathcal{I}_{wbf}(G) \leq O(G) - \Delta_e(G)$.

IV. EXAMPLES FOR TOTAL STRONG DOMINATION BIPOLAR INTUITIONISTIC FUZZY GRAPH

In this section we will provide examples of total strong domination bipolar intuitionistic fuzzy graphs illustrated by figures (Fig.4, Fig.5 and Fig.6), respectively.
Example 4.2

Fig. 5. Total Strong Domination Bipolar Intuitionistic Fuzzy Graphs.
V. CONCLUSION

Through this article, total strong (weak) domenation, strong (weak) bipolar intuitionistic fuzzy graphs and some properties are discussed. In Over future paper these concepts will be generalized to hyper and tripolar fuzzy soft set, also this concept will be used in developing some topics in many papers such as [25-27].

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