Predicting Strength Ratio of Laminated Composite Material with Evolutionary Artificial Neural Network

Huiyao Zhang¹, Atsushi Yokoyama²
Department of Fiber Science and Engineering
Kyoto Institute of Technology
Kyoto, JAPAN

Abstract—In this paper, an alternative methodology to obtain the strength ratio for the laminated composite material is presented. Traditionally, classical lamination theory and related failure criteria are used to calculate the numerical value of strength ratio of laminated composite material under in-plane and out-of-plane loading from a knowledge of the material properties and its layup. In this study, to calculate the strength ratio, an alternative approach is proposed by using an artificial neural network, in which the genetic algorithm is proposed to optimize the search process at four different levels: the architecture, parameters, connections of the neural network, and active functions. The results of the present method are compared to those obtained via classical lamination theory and failure criteria. The results show that an artificial neural network is a feasible method to calculate the strength ratio concerning in-plane loading instead of classical lamination and associated failure theory.

Keywords—Classical lamination theory; genetic algorithm; artificial neural network; optimization

I. INTRODUCTION

Fiber-reinforced composite materials have gained increasing attention due to their superior mechanical performance in stiffness, strength, and specific gravity of fibers over conventional materials. Laminated composite material takes advantage of fiber-reinforced composite material, and finds wide application in a variety of applications, which include electronic packaging, sports equipment, homebuilding, medical prosthetic devices, high-performance military structures, etc. The mechanical properties of composite laminated are determined by stacking sequence, ply thickness, fiber orientation, and material for each ply. Strength ratio[1], [2], [3], [4], [5], [6], [7], [8] is a critical index to predict the performance of a laminated composite material. There are two approaches for solving this problem: analytical methods, such as classical lamination theory(CLT); data-driven methods, such as artificial neural networks (ANN).

The analytical approach involves a two-step procedure to obtain strength ratio: first, develop the stress and strain relationship among in-plane loading using classical lamination theory based on a knowledge of the composite laminate properties of the individual layers and the laminate geometry; then calculate the strength ratio according to associated failure criteria, such as Tsai-Wu failure criterion, based on the above-obtained stress and strain relationship. However, the use of CLT needs intensive computation since it involves massive matrix multiplication and integration operation.

The other approach to this problem is using an artificial neural network, which is a data-driven method, instead of an analytical method. ANN, heavily inspired by biology and psychology, is a reliable tool instead of a complicated mathematical model, which can accelerate the calculation process and reduce the computation cost. It has been widely used to solve various practical engineering problems in applications [9], [10], such as pattern recognition, nonlinear regression, data mining, clustering, prediction, etc. Evolutionary artificial neural networks are a subclass of artificial neural networks, in which evolutionary algorithms are introduced to design the topology of an ANN. For an artificial neural network, the number of layers, the connection between neurons, the activation functions used in every neuron, etc. are critical components to its performance. The design of an ANN can be treated as an optimization procedure of discrete variables, which can be solved by a genetic algorithm (GA). It is claimed that the combinations of artificial neural networks and evolutionary algorithm [11] can significantly improve the performance of intelligent systems than that rely on ANNs or evolutionary algorithms alone.

GA, inspired by Darwin’s principle of survival of the fittest, is widely adopted to obtain the global optimal for discrete optimization problems. The techniques used in this algorithm, such as selection, crossover, mutation, are derived from natural selection, and individuals with better fitness get more chances to breed. Therefore, GA can be integrated into the design of ANN, in which encoding the information of an artificial neural network into a chromosome [12], [13].

The rest of this paper is organized as the following: Section II introduces the CLT and the failure criteria, which is used to check whether the composite material fails or not in the present study; Section III covers the design of an artificial neural network for a function approximation; Section IV reviews the use of the genetic algorithm in the design of neural network architecture, and the techniques of parameters optimization during the training process; Section V presents the result of the numerical experiments in different cases; in the conclusion part, we present and discuss the experiment results.

II. CLASSICAL LAMINATION THEORY AND FAILURE CRITERIA

A. Classical Lamination Theory

Classical lamination theory derives from three simplifying assumptions in laminated composite material: the laminate consist of plies bonded together through the thickness, the thickness of each ply is small, and it is consists of homogeneous, orthotropic material; the entire laminated composite
The stress-strain relation in local axis 1-2 is dimensional stress-strain equations can be reduced to two-from external loading. According to Hooke’s law, the three-angle ply laminate is as shown in Fig. 2. 

A few cases of laminates, such as symmetric laminates, cross-ply laminates, play an important role in the application of laminated composite material. A laminate is called an angle ply laminate if it has plies of the same material and thickness of laminated composite material. A laminate is called an angle cross-ply laminates, play an important role in the application called the global axis.

1) Stress and Strain in a Lamina: For a single lamina under in-plane loading whose thickness is relatively small, suppose the upper and lower surfaces of the lamina are free from external loading. According to Hooke’s law, the three-dimensional stress-strain equations can be reduced to two-dimensional stress-strain equations in the composite material. The stress-strain relation in local axis 1-2 is

$$\begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \tau_{12} \end{bmatrix} = \begin{bmatrix} Q_{11} & Q_{12} & 0 \\ Q_{12} & Q_{22} & 0 \\ 0 & 0 & Q_{66} \end{bmatrix} \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \gamma_{12} \end{bmatrix},$$

(1)

where \(Q_{ij}\) is the stiffness of a lamina. And they are related to engineering elastic constants as follows:

$$\begin{align*}
Q_{11} &= \frac{E_1}{1-v_{12}v_{21}}, \\
Q_{22} &= \frac{E_2}{1-v_{12}v_{21}}, \\
Q_{66} &= \frac{E_1}{1-v_{12}v_{21}}, \\
Q_{12} &= \frac{v_1 E_2}{1-v_{12}v_{21}},
\end{align*}$$

(2)

where \(E_1, E_2, v_{12}, G_{12}\) are four independent engineering elastic constants, which are defined as follows: \(E_1\) is the longitudinal Young’s modulus, \(E_2\) is the transverse Young’s modulus, \(v_{12}\) is the major Poisson’s ratio, and \(G_{12}\) is the in-plane shear modulus.

![Fig. 1. The Left Diagram Shows the Local and Global Axis of an Angle Lamina, which is from a Laminate as Shown in the Right Diagram.](image)

Stress-strain relation in the global x-y axis is

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{bmatrix} = \begin{bmatrix} Q_{11} & Q_{12} & Q_{16} \\ Q_{12} & Q_{22} & Q_{26} \\ Q_{16} & Q_{26} & Q_{66} \end{bmatrix} \begin{bmatrix} \varepsilon_x \\ \varepsilon_y \\ \gamma_{xy} \end{bmatrix},$$

(3)

where

$$\begin{align*}
Q_{11} &= Q_{11}\cos^2\theta + Q_{22}\sin^2\theta + 2(Q_{12} + 2Q_{66})\sin\theta\cos\theta, \\
Q_{12} &= (Q_{11} + Q_{22} - 4Q_{66})\sin\theta\cos\theta + Q_{12}(\cos^2\theta + \sin^2\theta), \\
Q_{22} &= Q_{11}\sin^2\theta + Q_{22}\cos^2\theta + 2(Q_{12} + 2Q_{66})\sin\theta\cos\theta, \\
Q_{16} &= (Q_{11} - Q_{12} - 2Q_{66})\sin^2\theta - (Q_{22} - Q_{12} - 2Q_{66})\sin\theta\cos\theta, \\
Q_{26} &= (Q_{11} - Q_{12} - 2Q_{66})\cos^2\theta - (Q_{22} - Q_{12} - 2Q_{66})\sin\theta\cos\theta, \\
Q_{66} &= (Q_{11} + Q_{22} - 2Q_{66})\sin^2\theta + Q_{66}\sin^2\theta + \cos^2\theta.
\end{align*}$$

(4)

2) Stress and Strain in a Laminate: For forces acting on laminates, such as in plate and shell structures, the relationship between applied forces and displacement can be given by

$$\begin{bmatrix} N_x \\ N_y \\ N_{xy} \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} & A_{16} \\ A_{12} & A_{22} & A_{26} \\ A_{16} & A_{26} & A_{66} \end{bmatrix} \begin{bmatrix} \varepsilon_0 \\ \varepsilon_\theta \\ \gamma_{xy} \end{bmatrix} + \begin{bmatrix} B_{11} & B_{12} & B_{16} \\ B_{12} & B_{22} & B_{26} \\ B_{16} & B_{26} & B_{66} \end{bmatrix} \begin{bmatrix} k_2 \\ k_4 \\ k_{xy} \end{bmatrix},$$

(5)

where \(N_x, N_y\) refers to the normal force per unit length; \(N_{xy}\) means shear force per unit length; \(\varepsilon_0\) and \(k_{xy}\) denotes midplane strains and curvature of a laminate in x-y coordinates. The mid-plane strain and curvature is given by

$$A_{ij} = \sum_{k=1}^{n} (Q_{ij})_k (h_k - h_{k-1})i = 1, 2, 6, j = 1, 2, 6,$$

$$B_{ij} = \frac{1}{2} \sum_{k=1}^{n} (Q_{ij})_k (h_k^2 - h_{k-1}^2)i = 1, 2, 6, j = 1, 2, 6,$$

$$D_{ij} = \frac{1}{3} \sum_{k=1}^{n} (Q_{ij})_k (h_k^3 - h_{k-1}^3)i = 1, 2, 6, j = 1, 2, 6.$$

The \([A], [B],\) and \([D]\) matrices are called the extensional, coupling, and bending stiffness matrices, respectively. The extensional stiffness matrix \([A]\) relates the resultant in-plane forces to the in-plane strains, and the bending stiffness matrix \([D]\) couples the resultant bending moments to the plane curvatures. The coupling stiffness matrix \([B]\) relates the force and moment terms to the midplane strains and curvatures.

B. Failure Criteria for a Lamina

Failure criteria for composite materials are more difficult to predict due to structural and material complexity. The failure process of composite materials can be regarded from microscopic and macroscopic points of view. The most popular criteria about the failure of an angle lamina are from the macroscopic point of view, which are according to the tensile, compressive, and shear strengths. As shown in Fig. 3, there are two types of failure criteria \([14], [15], [16], [17], [18], [19], [20], [21]\) according to failure surfaces. The first failure surface is a rectangle that includes the maximum stress failure criterion \([22]\), and maximum strain failure criterion. The second failure surface is ellipsoidal that includes Tsai-Wu \([23], [24]\), Chamis, Hoffman, and Hill criteria. In the present study, the two most
reliable failure criteria are adopted, Maximum stress and Tsai-Wu. Both these failure criteria are based on the stress in the local axis instead of principal normal stress and maximum shear stresses, in which four normal strength parameters and one shear stress are involved. The five strength parameters are:

\[(\sigma^T_{1})_{ult} = \text{ultimate longitudinal tensile strength in direction 1},\]
\[(\sigma^C_{1})_{ult} = \text{ultimate longitudinal compressive strength},\]
\[(\sigma^T_{2})_{ult} = \text{ultimate transverse tensile strength},\]
\[(\sigma^C_{2})_{ult} = \text{ultimate transverse compressive strength},\]
\[(\tau_{12})_{ult} = \text{and ultimate in-plane shear strength}.\]

1) **Maximum stress (MS) failure criterion:** Maximum stress failure criteria consist of the normal stress theory and the shear stress theory. The stress applied to a lamina can be resolved into the normal stress and shear stress in the local axis. The lamina fails if either of the normal stress or shear stress in the local axis of a lamina is equal or exceeds the corresponding ultimate strengths of the unidirectional lamina. That is,

\[\sigma_1 \geq (\sigma^T_{1})_{ult} \quad \text{or} \quad \sigma_1 \leq -(\sigma^C_{1})_{ult},\]
\[\sigma_2 \geq (\sigma^T_{2})_{ult} \quad \text{or} \quad \sigma_2 \leq -(\sigma^C_{2})_{ult},\]
\[\tau_{12} \geq (\tau_{12})_{ult} \quad \text{or} \quad \tau_{12} \leq -(\tau_{12})_{ult},\]

where \(\sigma_1\) and \(\sigma_2\) are the normal stresses in the local axis 1 and 2; \(\tau_{12}\) is the shear stress in the symmetry plane 1-2.

2) **Tsai-Wu failure criterion:** The Tsai-Wu criterion is one of the most reliable static failure criteria derived from the von Mises yield criterion. A lamina is considered to fail if

\[H_1 \sigma_1 + H_2 \sigma_2 + H_6 \tau_{12} + H_{11} \sigma^2_1 + H_{22} \sigma^2_2 + H_{66} \tau_{12}^2 + 2H_{12} \sigma_1 \sigma_2 < 1\]

is violated, where

\[H_1 = \frac{1}{(\sigma^T_{1})_{ult}} - \frac{1}{(\sigma^C_{1})_{ult}},\]
\[H_{11} = \frac{1}{(\sigma^T_{1})_{ult} (\sigma^C_{1})_{ult}},\]
\[H_2 = \frac{1}{(\sigma^T_{2})_{ult} (\sigma^C_{2})_{ult}},\]
\[H_{22} = \frac{1}{(\sigma^T_{2})_{ult} (\sigma^C_{2})_{ult}},\]
\[H_{66} = \frac{1}{(\tau_{12})_{ult}^2},\]
\[H_{12} = -\frac{1}{2} \sqrt{(\sigma^T_{1})_{ult} (\sigma^C_{1})_{ult} (\sigma^T_{2})_{ult} (\sigma^C_{2})_{ult}}.\]

\(H_i\) is the strength tensor of the second-order; \(H_{ij}\) is the strength tensor of the fourth-order. \(\sigma_1\) is the applied normal stress in direction 1; \(\sigma_2\) is the applied normal stress in direction 2; \(\tau_{12}\) is the applied in-plane shear stress.

3) **Strength ratio:** The safety factor, or yield stress, is how much extra load beyond is intended a composite laminate will take. The strength ratio\(\text{SR}\) is defined as

\[SR = \frac{\text{Maximum Load Which Can Be Applied}}{\text{Load Applied}}.\]

### III. EVOLUTIONARY ARTIFICIAL NEURAL NETWORK

#### A. General Neural Network

In this paper, the feedforward ANN is adopted in the current study, since it is straightforward to code. For function approximation through an artificial neural network, Cybenko demonstrated that a two-layer perceptron can form an arbitrarily close approximation to any continuous nonlinear mapping [25]. Therefore, a two-layer feedforward ANN is proposed in the present study. Fig. 4 shows a general framework for a two-layer ANN, in which the number of nodes in the hidden layer and the connection with inputs, are critical in the design of an ANN. The nodes in the hidden layer are treated as feature extractors or detectors. Therefore, nodes within this layer should partially be connected with the inputs of an ANN, since the unnecessary connections would increase the model’s complicity, which will reduce an ANN’s performance. The number of nodes in the hidden layer should be less than the number of inputs since the nodes in the hidden layer are features. For the nodes in the last layer, every node should be fully connected with nodes in the previous layer, the relationship between the outputs and features should be direct. The rest, which affects the performance of an artificial neural network, are the activation function, and ANNs training method. In the following section, the \(i\)th node in the input layer is denoted as \(i_i\), and the \(j\)th node in the hidden layered denoted as \(h_j\), respectively.

#### B. Activation Function

The activation function is one of the critical parts of an ANN. Liu [12] et al. claims that the performance of neural
networks with different activation functions is different, even if they have the same architecture. A generalized activation function can be written as

\[ y_i = f\left(\sum_{j=1}^{n} w_{ij}x_j - \theta\right) \quad (11) \]

where \( y_i \) is the output of the node \( i \), \( x_j \) is the \( j \)th input to the node, and \( w_{ij} \) is the connection weight between adjacent nodes \( i \) and \( j \). Table I display the most widely adopted activation functions in the design of an ANN, which is used in the current study.

C. Weights Learning

The weight training in an ANN is to minimize the error function, such as the most widely used mean square error function, which calculates the difference between the desired and the prediction output values averaged overall examples. Gradient descent algorithm is widely adopted to reduce the value of an error function, which has been successfully applied in many practical areas. However, this class of algorithms is plagued by the possible existence of local minima or “flat spots” and “the curse of dimensionality”. One method to overcome this problem is to adopt a genetic algorithm.

IV. METHODOLOGY

For an angle ply laminate, its strength ratio can be computed based on Tsai-Wu failure theory or maximum stress theory given the laminate’s lay-up, material properties, in-plane loading, etc. To model this function, we propose an ANN framework as shown in Fig. 6, which derives from the previous two-layer model. There are sixteen inputs of this ANN, which are in-plane loading \( N_x, N_y, \) and \( N_{xy} \); design parameters of a laminate, two fiber orientation \( \theta_1 \) and \( \theta_2 \), ply thickness \( t \), total number of plies \( N \); five engineering constants of composite materials, \( E_1, E_2, G_{12}, \) and \( v_{12} \); five strength parameters of a unidirectional lamina. Two outputs are strength ratio according to MS theory and strength ratio according to Tsai-Wu theory.

The work involved in the evolution process of ANN consists of three parts: search space, which includes the topology of an ANN, activation function, etc.; search strategy, which details how to explore the search space; performance estimation strategy refers to the measurement of the performance of an artificial neural network.

A. Search Space

We propose a general neural network framework as shown in Fig. 4. The search space is parameterized by four parts: (1) the number of nodes \( m \) (possibly unbounded) in the hidden layer, to further narrow down the search space, the assumption is \( m \) less than \( n \); (2) the type of operation every node executes, e.g., sigmoid, linear, Gaussian; (3) the connection relationship between the hidden nodes and inputs (4) the weight value in the connection if a connection exists.

Therefore, the evolution process in an evolutionary artificial neural network can be divided into four different levels: topology, learning rules, active functions, and connection weights. For the evolution of the topology, the aim is to find an optimal ANN architecture for a specific problem. The architecture

![Fig. 4. Network Diagram for the Two-layer Neural Network. The Input, Hidden, and Output Variables are Represented by Nodes, and the Weight Parameters are Represented by Links between the Nodes. Arrows Denote the Direction of Information Flow Through the Network During Forward Propagation.](image-url)

**Fig. 4.** Network Diagram for the Two-layer Neural Network. The Input, Hidden, and Output Variables are Represented by Nodes, and the Weight Parameters are Represented by Links between the Nodes. Arrows Denote the Direction of Information Flow Through the Network During Forward Propagation.

**Fig. 5.** A General Framework for Evolutionary Neural Network, in which Fitness Refers to the Corresponding Value of Objective Function.

<table>
<thead>
<tr>
<th>Type</th>
<th>Description</th>
<th>Formula</th>
<th>Range</th>
<th>Encoding</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear</td>
<td>The output is proportional to the input</td>
<td>( f(x) = cx )</td>
<td>((-\infty, +\infty))</td>
<td>00</td>
</tr>
<tr>
<td>Sigmoid</td>
<td>A family of S-shaped functions</td>
<td>( f(x) = \frac{1}{1 + e^{-x}} )</td>
<td>((0, 1))</td>
<td>01</td>
</tr>
<tr>
<td>ReLU</td>
<td>A piece-wise function</td>
<td>( f(x) = \min{0, x} )</td>
<td>((0, +\infty))</td>
<td>10</td>
</tr>
<tr>
<td>Softplus</td>
<td>A family of S-shaped functions</td>
<td>( f(x) = ln(1 + e^x) )</td>
<td>((0, +\infty))</td>
<td>11</td>
</tr>
</tbody>
</table>

**TABLE I. EXAMPLES OF WIDELY USED ACTIVATION FUNCTIONS IN THE DESIGN OF AN ARTIFICIAL NEURAL NETWORK**

The work involved in the evolution process of ANN consists of three parts: search space, which includes the topology of an ANN, activation function, etc.; search strategy, which details how to explore the search space; performance estimation strategy refers to the measurement of the performance of an artificial neural network.
TABLE II. THE BINARY REPRESENTATION OF PARENT 1, PARENT 2, AND CHILD CORRESPONDING TO FIG. 7(A), (B), AND (C), WITH $i_1, i_2, \ldots , i_{16}$ DENOTE SIXTEEN INPUTS AND $h_1, h_2, \cdots , h_{12}$ REFER TO NODES IN THE HIDDEN LAYER. 1 REPRESENTS AN EDGE FROM THE INPUT NODE TO THE HIDDEN NODE, AND 0 REPRESENTS NO EDGE FROM THE INPUT NODES TO THE HIDDEN NODE.

<table>
<thead>
<tr>
<th>Hidden Nodes</th>
<th>$i_1$</th>
<th>$i_2$</th>
<th>$i_3$</th>
<th>$i_4$</th>
<th>$i_5$</th>
<th>$i_6$</th>
<th>$i_7$</th>
<th>$i_8$</th>
<th>$i_{10}$</th>
<th>$i_{11}$</th>
<th>$i_{12}$</th>
<th>$i_{13}$</th>
<th>$i_{14}$</th>
<th>$i_{15}$</th>
<th>$i_{16}$</th>
<th>$f$</th>
<th>$f$</th>
</tr>
</thead>
<tbody>
<tr>
<td>P1</td>
<td>$h_1$</td>
<td>1 1 1 1 1 1 0 0 0 0 0 0 1 1 0 0</td>
<td>0 0 0 0 1 0 1 1 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_2$</td>
<td>0 1 1 1 1 0 0 1 0 0 1 0 1 1 0 0 0 0 0 0 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_3$</td>
<td>1 0 0 1 0 1 1 0 1 1 0 0 1 0 0 0 0 0 0 0 0 0 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_4$</td>
<td>0 0 1 0 1 0 0 0 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_5$</td>
<td>0 0 0 0 0 0 1 0 1 0 1 0 1 1 1 1 0 0 0 0 0 0 0 0 0 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>P2</td>
<td>$h_1$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 1 0 0 0 0 0 0 0 0 0 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_2$</td>
<td>1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_3$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_4$</td>
<td>0 0 1 1 1 1 1 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_5$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_6$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_7$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_8$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_9$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_{10}$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_{11}$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_{12}$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Child</td>
<td>$h_1$</td>
<td>1 1 1 1 1 1 0 0 0 0 0 0 0 0 1 1 0 0 0 0 1 1 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_2$</td>
<td>0 1 1 1 1 0 0 0 1 0 0 1 1 0 0 0 0 0 0 0 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_3$</td>
<td>0 0 0 0 0 0 1 1 1 1 1 1 0 0 0 0 0 0 0 1 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_4$</td>
<td>0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_5$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$h_6$</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
The crossover between individuals results in exploiting the area between the given two-parent solutions. In the present study, we search the local area by combining the genes of the corresponding equation to get the strength ratio. Repeat this procedure to yield 14000 points uniformly distributed over the domain space, and define the domain of the corresponding inputs as follows: the range of in-plane loading varies from 0 to 120; the range of fiber orientation θ is from -90 to 90; ply thickness t is 1.27mm, the number of plies ranges N from 4 to 120. Three different composite material is used in this experiment, as shown in Table III. Table IV shows part of the training data, which are randomly selected from the generated training dataset. To speed up the learning and accelerate convergence, the input attributes of the dataset are rescaled to between 0 and 1.0 by a linear function.

**C. Performance Estimation Strategy**

The simplest approach to this problem is to perform standard training and validation of the architecture on a dataset. However, this method is inefficient and computationally intensive. Therefore, many recent research [26] focuses on developing strategies reducing the cost of performance estimation. In this work, during the GA process, we adopt the following straightforward and efficient method to estimate the performance of an ANN: first, train a neural network one hundred times on the training dataset; second, do the validation test; measure the neural network’s performance according to its fitness of objective function on the test dataset.

**V. Experiment**

In the previous section, we present the details of our strategies for designing an ANN. In this section, we explain the details of the preparation of the training dataset and validation dataset.

**A. Dataset Preparation**

For composite material, it is impossible to obtain massive training data from the practical scenario. Therefore, we use classical lamination theory and failure theory, which follows a two-step procedure: first, evaluate the stress and strain according to classical lamination theory; second, substitute them into the corresponding equation to get the strength ratio. Repeat this procedure to yield 14000 points uniformly distributed over the domain space, and define the domain of the corresponding inputs as follows: the range of in-plane loading varies from 0 to 120; the range of fiber orientation θ is from -90 to 90; ply thickness t is 1.27mm, the number of plies ranges N from 4 to 120. Three different composite material is used in this experiment, as shown in Table III. Table IV shows part of the training data, which are randomly selected from the generated training dataset. To speed up the learning and accelerate convergence, the input attributes of the dataset are rescaled to between 0 and 1.0 by a linear function.

**B. ANN Training and Validation**

The ANN training procedure is carried out by optimizing the multinomial logistic regression objective using mini-batch gradient descent [27] with momentum. The batch size is set to 1000, momentum to 0.9, the learning rate is set to 10^{-2}. The ratio of the training dataset and validation dataset is 70/30, with 70% of the entire data for training and 30% for validation.

**C. Genetic Algorithm**

The genetic algorithm involves the evolution of an artificial neural network’s topology, activation function, etc. in the optimizing process. The corresponding parameters are as follows:

The population is 10, the percentage of parents in the crossover operator: Fig. 7(c) is the child of Fig. 7(a) and (b), child c inherits the connection relationship part of the training data, which are randomly selected from the generated training dataset. To speed up the learning and accelerate convergence, the input attributes of the dataset are rescaled to between 0 and 1.0 by a linear function.
VI. RESULT AND DISCUSSION

In this work, we propose to use an artificial neural network as an alternative way to compute the strength ratio of composite material instead of a two-step procedure, based on classical lamination and failure theory. Fig. 8 shows the changes of the fitness and error during the evolution procedure. The fitness is obtained through the performance estimation technique of an artificial neural network. As shown in this figure, fitness grows during the initial stage; then, it slowly converges as generation proceeds. It implies genetic algorithm can find a better artificial neural network with the evolution of the number of neurons in the hidden layer, connection relationship, activation functions, and connection weights.

Fig. 9 shows the rest training of the artificial neural network obtained from the GA, which is a pre-trained ANN. Continue to train it with a standard gradient-based descent algorithm until the error converges. The target neural network converges rapidly at first, and further training doesn’t reduce the error efficiently. Then, this artificial neural network is used to predict the strength ratio of laminated composite material.

To present the evaluation result of the ANN straightforwardly, several experiment results from the validation dataset are displayed in Table V, which are randomly selected. Comparing the strength ratio outputs based on CLT and ANN from Table V, it is shown that the calculation of strength ratio can be achieved using a two-layer neural network, without the intensive computation of matrix multiplication.

VII. CONCLUSION

In this paper, an evolutionary artificial neural network model was developed to predict the strength ratio of laminated composite material under in-plane loading. We review the use of genetic algorithms and artificial neural networks as an alternative approach for calculating the strength ratio of an angle ply laminate under in-plane loading. Traditionally, it is obtained through CLT and corresponding failure criteria, such as Maximum Stress theory and Tsai-Wu failure theory.

The main contribution of this work is as follows: 1) propose a two-layer diagram model for designing a sophisticated neural network in simulating the calculation of strength ratio, and use a genetic algorithm to explore the search space; 2) suggest an efficient method to compute the strength ratio instead of adopting the two-step procedure based on classical lamination theory and related failure criteria. Compared with experimentally obtained data, it is demonstrated that ANN is an efficient and simple tool to compute the strength ratio, instead of the complex analytical mathematical model. Our findings underline the practical applicability of ANN on the analysis of composite material.

There are more improvements we can make over the search strategy and application in the area of laminated composite material. The future work is to develop a more sophisticated ANN, which not only can predict the properties for angle ply laminate, but also the other type of laminated composite material.

ACKNOWLEDGMENT

The work has partly been supported by China Scholarship Council(CSC) under grant no. 201806630112

REFERENCES


