

# Method for Image Source Separation by Means of Independent Component Analysis: ICA, Maximum Entropy Method: MEM, and Wavelet Based Method: WBM

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**Abstract**—Method for image source separation based on Independent Component Analysis: ICA, Maximum Entropy Method: MEM, and Wavelet Based Method: WBM is proposed. Experimental results show that image separation can be done from the combined different images by using the proposed method with an acceptable residual error.

**Keywords**—Blind separation; image separation; cucktail party effect; ICA; MEM; wavelet analysis.

## I. INTRODUCTION

There are some technologies and systems which allow separate the specific speaker from the mixed image data which is acquired at some noisy circumstances. The related application studies are conducted, in particular, for TV meeting environment, image recognition systems, and digital hearing aid system etc. In particular, the microphone array system as well as Independent Component Analysis (ICA) base approach [1] is focused. Microphone array allows enhance a target image from the mixed images suppressing noises and taking into account the phase difference among the imagesources which corresponds to the distance between the microphone and the location of the imagesources. There is a delay sum [2] and an adaptation [3] types array microphone systems. These types of array microphone allow direct the beam to the desired direction of the target of interest.

ICA is the method which allows the blind separation based on the imagesources are isolated each other. ICA based method configures reconstruction filter maximizing Kullback-Leibler Divergence [4] for separation of target imagesources in concern from the acquired images [5], [6].

The blind separation method with entropy maximization rule is proposed [7]. In order to improve separability among the possible imagesources, high frequency component derived from the wavelet based Multi Resolution Analysis (MRA) [8],[9] is used in the entropy maximization rule utilized method. Due to the fact that the MRA based separability improvement is not good enough, further improvement is required.

Blind separation method which is proposed here is based on the MRA based separability improvement. A single level of MRA is not good enough for characteristics enhancement of each imagesource. Therefore, the level is considered as a parameter for MRA utilized blind separation [10]. An appropriate level is found for improvement of separability then blind separation is applied. It is found that the proposed method can achieve 4 to 8.8% of separability improvement for the case of the number of speakers is 2, 4 and 8 [11].

The following section describes the proposed method followed by some experiments with the mixed images. Then conclusions and some discussions is followed.

## II. PROPOSED MTHEOD

### A. Image Mikxing Model

Assuming the original image,  $x_i(t)$  is mixed with several images, for instance  $s_1(t)$  and  $s_2(t)$  as shown in equation (1).

$$x_i(t) = a_{i1}s_1(t) + a_{i2}s_2(t) \quad (1)$$

where  $a_{i1}$  and  $a_{i2}$  are weighting factor, mixing ratio. Also it is assumed that  $s_1(t)$  and  $s_2(t)$  are mutually independent. Although this is an example of image mixing model for just two images, it is possible to expand the number of images which are to be mixed together.

### B. Maximum Entropy Method

Maximum Entropy Method: MEM is used for learning processes for maximizing combined entropy in two layered neural network

$$y_i = g(\sum_{k=1}^2 w_{ik} x_k - \theta_i) \quad (2)$$

$$g(v) = 1 - e^{-v} / (1 + e^{-v}) \quad (3)$$

where  $x, y$  notes input and output signals, or images while  $w$  denotes weighting coefficients of two layered neural network.  $\theta$  denotes a threshold.  $g(v)$  is called sigmoid function.

The combined entropy can be expressed with the equation (4).

$$H(y) = \langle \ln(|J|) \rangle - \langle \ln(p(x)) \rangle \quad (4)$$

where  $J$  denotes Jacobian matrix as shown in equation (5)

$$J = \det \begin{pmatrix} \partial y_1 / \partial x_1 & \partial y_1 / \partial x_2 \\ \partial y_2 / \partial x_1 & \partial y_2 / \partial x_2 \end{pmatrix} \quad (5)$$

Because the second term of the equation (4) is constant, the following equation (6) has to be maximized.

$$I = - \langle \ln(|J|) \rangle \quad (6)$$

### C. Steepest Descending Method

In order to maximize the equation (6), Steepest Descending Method: SDM is used. Updating equations for  $w$  and  $\theta$  can be expressed with equations (7) and (8).

$$w_{ik}^{new} = w_{ik}^{old} - \gamma \partial I / \partial w_{ik} \quad (7)$$

$$\theta_i^{new} = \theta_i^{old} - \gamma \partial I / \partial \theta_i \quad (8)$$

More precisely, updating equations can be re-written by equation (9) and (10).

$$W^{new} = W^{old} + \gamma \langle [W^T]^{-1} + 2yx^T \rangle \quad (9)$$

$$\theta^{new} = \theta^{old} + \gamma \langle 2y \rangle \quad (10)$$

Thus the original images are separated from the combined image with the proposed method.

### D. Discrete Wavelet Transformation

In order to separate several original images from the given combined images, Discrete Wavelet Transformation: DWT is used. DWT allows decompose images with high and low wavelet frequency components orthogonally. There are many orthogonal base functions for DWT. One of the based functions is Haar function. Figure 1 shows an example of the original image of Lena in the SIDBA standard image database, and decomposed image through WT. In the decomposed image, LL image, low frequency component in horizontal direction and low frequency component in vertical direction is situated at the top left corner while LH, HL, and HH components are situated at the top right, the bottom left, and the bottom right corners, respectively.

Histogram of the low frequency component is shown in Figure 2 (a) while that of the high frequency component is shown in Figure 2 (b). This histogram is for the decomposed image of Lena image. The histogram (a) is for LL component while the histogram (b) is for HH component. The histogram of the high frequency component looks similar to normal distribution and is mainly concentrated at the wavelet frequency component ranges from 0 to 10 wavelet frequency. On the other hand, Histogram of the LL component does not look like normal distribution.



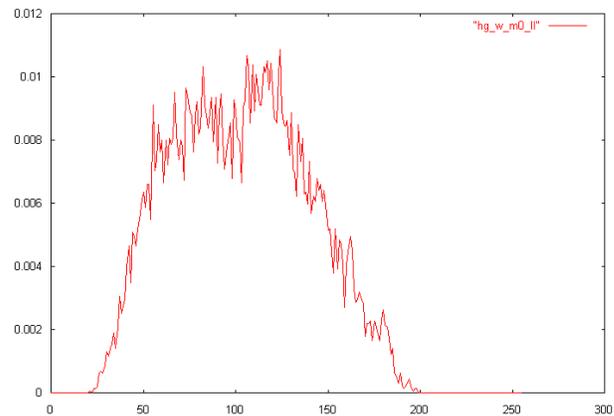
(a)Original image



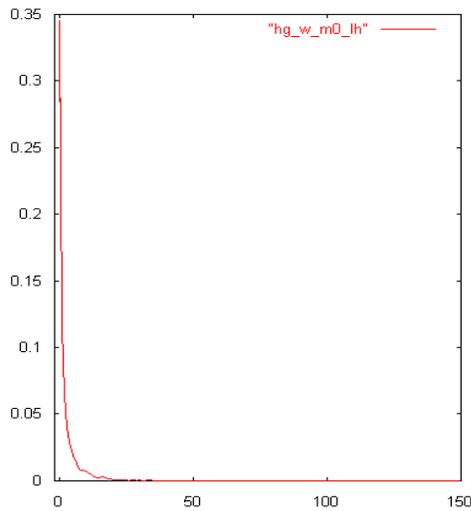
(b)Decomposed image

Figure 1 Example of original and decomposed images with DWT.

These histogram characteristics are common to original image and differ from each other depending on natures of the original images. Therefore, it is possible to separate original images using the difference of histograms of the decomposed image derived through DWT.



(a)Low Frequency Component



(b)High Frequency Component

Figure 2 Histograms of high and low frequency components of the decomposed image after DWT

### III. EXPERIMENTS

#### A. Original Images Used

Figure 3 shows two original images, Lena, and Barbara in the same standard image database, SIDBA.



(a)Lena



(b)Barbara

Figure 3 Two original images used for experiments

Also examples of mixed images are shown in Figure 4. Mixing ratios of Figure 4 (a) and (b) are different. Mixing ratio of Figure 4 (a) is 90% of Lena image and 10% of Barbara image while that of Figure 4 (b) is 10% of Lena image and 90% of Barbara image. Image As shown in Figure 4, image defects are found on the mixed, combined images.

Figure 5 shows DWT applied images of Figure 4 of combined images.



(a)Combined image with 90% of Lena and 10% of Barbara



(b) Combined image with 90% of Barbara and 10% of Lena  
Figure 4 Combined images with the different mixing ratios



(b) DWT image of Figure 3 (b) of combined image

Figure 5 DWT images of Figure 4.



(a) DWT image of Figure 3 (a) of combined image

### B. Separated Images with the Different Mixing Ratios

Mixed image between Lena and Barbara images with the different mixing ratios, 50%, 30%, and 10% are created. Using the proposed method, separation of each original image is attempted. Resultant images are shown in Figure 6, 7, and 8 for the mixing ratios, 50%, 30%, and 10%, respectively. As shown in these Figures, image separation performance depends on the mixing ratio. It is difficult to separate image when the mixing ratio is around 50%. Meanwhile, image separation performance is getting better in accordance with decreasing of the mixing ratio. In particular, the separated images for the mixing ratio of 10% are almost perfect, look extremely similar to the original images.



(a)



(b)

Figure 6 Separated images in the case of which mixing ratio is 50%.



(b)

Figure 7 Separated images in the case of which mixing ratio is 30%.



(a)



(a)



(b)

Figure 8 Separated images in the case of which mixing ratio is 10%.

#### IV. CONCLUSION

Method for image source separation based on Independent Component Analysis: ICA, Maximum Entropy Method: MEM, and Wavelet Based Method: WBM is proposed. Experimental results show that image separation can be done from the combined different images by using the proposed method with an acceptable residual error.

It is found that the image separation performance depends on the mixing ratio. It is difficult to separate image when the mixing ratio is around 50%. Meanwhile, image separation performance is getting better in accordance with decreasing of the mixing ratio. In particular, the separated images for the mixing ratio of 10% are almost perfect, look extremely similar to the original images.

#### ACKNOWLEDGMENT

The author would like to thank Takeshi Yoshida for his effort to the experiments.

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